

Spring Block 1

**Multiplication  
and division B**

## Small steps

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## Small steps

Step 9

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# Multiples of 10

## Notes and guidance

Children learnt the 10 times-table in Year 2 and revisited multiples of 10 in the Autumn term. In this small step, they further develop their understanding of multiples of 10 by looking at greater multiples.

Children reinforce their earlier work on place value and use a range of representations, such as ten frames, Gattegno charts and place value charts. They recognise that multiples of 10 end in a zero and use this fact to solve basic multiplication and division problems beyond the 10 times-table.

Understanding multiples of 10 is crucial for the next step, when children explore multiplying by 20, 30 and so on. This is the foundation of multiplying other 2-digit numbers using the expanded method later in this block and for more formal methods in Year 4 and beyond.

## Things to look out for

- Children may think that multiplying by 10 is always equivalent to adding a zero, rather than considering place value, which could lead to misconceptions in later years when they multiply decimals.
- Children may need support to recognise when to multiply and when to divide by 10

## Key questions

- What is the multiple of 10 before \_\_\_\_\_?
- What is the multiple of 10 after \_\_\_\_\_?
- Is \_\_\_\_\_ a multiple of 10? How can you tell?
- How many tens are there in \_\_\_\_\_?
- How can you use a Gattegno chart/place value chart to help multiply or divide a number by 10?
- What is the same about all multiples of 10? What is different?

## Possible sentence stems

- I know \_\_\_\_\_ is a multiple of 10 because ...
- \_\_\_\_\_ multiplied by 10 is equal to \_\_\_\_\_
- \_\_\_\_\_ is 10 times the size of \_\_\_\_\_
- There are \_\_\_\_\_ tens in \_\_\_\_\_

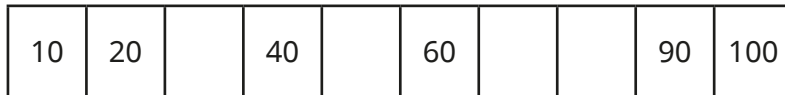
## National Curriculum links

- Recall and use multiplication facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers (Y2)

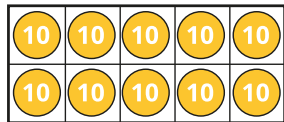
# Multiples of 10

## Key learning

- Complete the number track.

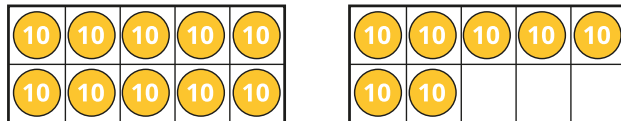


- Use the ten frame to complete the sentence.



10 tens are equal to \_\_\_\_\_

Use the ten frames to complete the calculation.



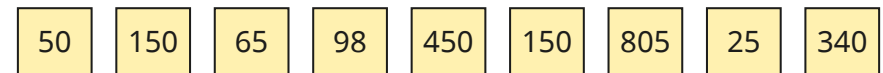
$$17 \times 10 = 10 \times 10 + 7 \times 10 = \underline{\quad} + \underline{\quad} = \underline{\quad}$$

- Work out the multiplications.

$14 \times 10$	$19 \times 10$	$23 \times 10$	$10 \times 26$
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- Dexter has 13 bags of marbles.  
There are 10 marbles in each bag.  
How many marbles does Dexter have altogether?

- Which of these numbers are multiples of 10?



Explain how you know.

- A bush is 4 m tall.  
A tree is 10 times as tall as the bush.  
How tall is the tree?

- Fill in the missing numbers.

▶ $23 \times 10 = \underline{\quad}$	▶ $\underline{\quad} \times 10 = 280$
▶ $64 \times \underline{\quad} = 640$	▶ $\underline{\quad} \times 10 = 420$

- A ribbon is 270 cm long.



- Ron wants to cut the ribbon into 10 cm pieces.  
How many pieces can he cut?

# Multiples of 10

## Reasoning and problem solving

Teddy saves £10 a week.  
 How many weeks will it take him to save £120?  
 How do you know?



12 weeks

Mr Trent has a piece of wood.



Mr Trent cuts it into three parts, A, B and C.

- Part A is 10 times as long as part C.
- Part B is 4 times as long as part C.
- Part A is 100 cm long.

How long was the piece of wood before Mr Trent cut it?

150 cm

Here is a Gattegno chart and a place value chart.

100	200	300	400	500	600	700	800	900
10	20	30	40	50	60	70	80	90
1	2	3	4	5	6	7	8	9

Hundreds	Tens	Ones

Show each number on both charts.

21	14	32	40	26
----	----	----	----	----

Multiply each number by 10  
 Show the results on the charts.

What is the same and what is different?



210, 140, 320,  
400, 260

## Related calculations

### Notes and guidance

This small step builds on the previous step and children's existing knowledge of times-tables to explore calculations related to known facts.

Children explore scaling facts by 10, for example using  $3 \times 4 = 12$  to derive  $3 \times 40 = 120$  and  $30 \times 4 = 120$ . A range of representations are used to expose the link between multiples of 1 and multiples of 10. Children begin by using base ten, before moving on to the slightly more abstract representation of place value counters. Children go on to explore this relationship with division, for example using  $12 \div 3 = 4$  to derive  $120 \div 3 = 40$ . This will be revisited later in the block.

Care should be taken to ensure that children do not also think that  $12 \div 30 = 40$ . This is a good opportunity to remind them that multiplication is commutative while division is not.

### Things to look out for

- Children may derive incorrect division facts by using the rules they have learnt about related multiplication facts.
- Children may try to find results by calculation rather than recognising the relationship between one fact and another.

### Key questions

- What is the same and what is different about the two calculations?
- How can you represent the calculation using place value counters/base 10?
- How is multiplying by 10s different from multiplying by 1s?
- What is the connection between the two calculations?

### Possible sentence stems

- \_\_\_\_\_  $\times$  \_\_\_\_\_ ones is equal to \_\_\_\_\_ ones,  
so \_\_\_\_\_  $\times$  \_\_\_\_\_ tens is equal to \_\_\_\_\_ tens.
- \_\_\_\_\_  $\div$  \_\_\_\_\_ is equal to \_\_\_\_\_,  
so \_\_\_\_\_ tens  $\div$  \_\_\_\_\_ is equal to \_\_\_\_\_ tens.

### National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

# Related calculations

## Key learning

- Complete the number sentences to match the pictures.

▶  $4 \times 2 \text{ ones} = \underline{\quad} \text{ ones}$

▶  $4 \times 2 = \underline{\quad}$

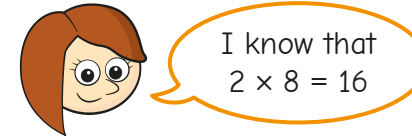
▶  $4 \times 2 \text{ tens} = \underline{\quad} \text{ tens}$

▶  $4 \times 20 = \underline{\quad}$

- Complete the multiplication facts.

$\underline{\quad} \times 4 = \underline{\quad}$

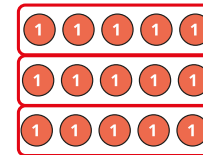
$\underline{\quad} \times 40 = \underline{\quad}$



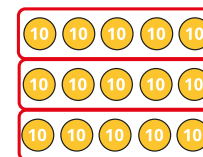
Use Rosie's fact to complete the multiplications.

▶  $2 \times 80 = \underline{\quad}$     ▶  $20 \times 8 = \underline{\quad}$     ▶  $8 \times 20 = \underline{\quad}$

- Use the place value counters to complete the divisions.



$15 \div 3 = \underline{\quad}$



$15 \text{ tens} \div 3 = \underline{\quad}$

- Use place value counters to help complete the calculations.

▶  $27 \div 9 = \underline{\quad}$     ▶  $54 \div 6 = \underline{\quad}$     ▶  $48 \div 4 = \underline{\quad}$

$270 \div 9 = \underline{\quad}$      $540 \div 6 = \underline{\quad}$      $480 \div 4 = \underline{\quad}$

- 4 family tickets to a theme park cost £240 in total.  
How much does 1 family ticket cost?



# Related calculations

## Reasoning and problem solving



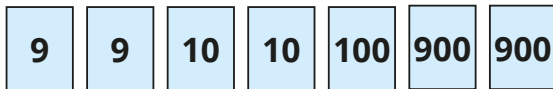
I know  
 $2 \times 6 = 12$ , so  
 $2 \times 60 = 120$

Tiny is correct.

Write the fact family for this multiplication.

$60 \times 2 = 120$   
 $120 \div 2 = 60$   
 $120 \div 60 = 2$

Use the number cards to complete the calculations.



You can use each card only once.

$900 \div \square = 100$   
 $\square \div \square = 9$   
 $\square \times \square = \square \div \square$

$900 \div 9 = 100$   
 $900 \div 100 = 9$   
 $9 \times 10 = 900 \div 10$

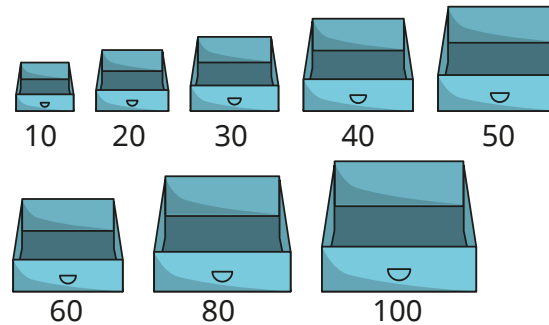
Scott has 240 cakes to sell.



He chooses one size of box and puts the same number of cakes in each box.

He has no cakes left over.

Which of these boxes could he use?



10, 20, 30, 40, 60 or 80

Is the statement true or false?

$5 \times 30 = 3 \times 50$

True

Explain your answer.



## Reasoning about multiplication

### Notes and guidance

In this small step, children develop their knowledge and understanding of the structure of multiplication.

Children begin by recapping what multiplication looks like with objects, and gradually use more abstract representations. These include cubes, base 10, arrays and number sentences. They use the symbols  $<$ ,  $>$  and  $=$  to compare groups using multiplication and division structures, both in context and within number sentences. Children are encouraged to realise that, for example,  $6 \times 3 > 6 \times 2$  without doing any calculation, but by recognising the relationship between the calculations and that the first must give an answer greater than the second because the same number is being multiplied by 3 and 2

### Things to look out for

- When comparing number sentences, children may find it difficult to recognise which digit is referring to the size of the group and which digit is referring to the number of groups.
- Children may try to work out the calculations to make comparisons, rather than using their understanding of the multiplicative structure.

### Key questions

- What number sentences are shown by the array?
- What is the same and what is different about  $8 \times 3$  and  $8 \times 4$ ?
- Which digit represents the size of the group?
- Which digit refers to the number of groups?
- What happens if you increase/decrease the number of groups?
- What happens if you increase/decrease the size of the groups?
- Do you need to complete the calculations to compare them?

### Possible sentence stems

- \_\_\_\_\_ lots of \_\_\_\_\_ is greater than \_\_\_\_\_ lots of \_\_\_\_\_
- \_\_\_\_\_ lots of \_\_\_\_\_ is less than \_\_\_\_\_ lots of \_\_\_\_\_
- I know that \_\_\_\_\_ is greater because ...

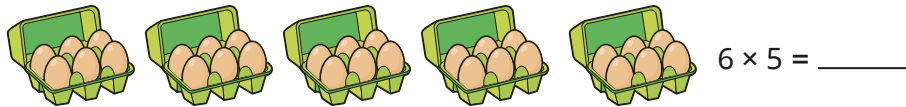
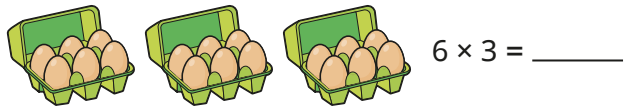
### National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

# Reasoning about multiplication

## Key learning

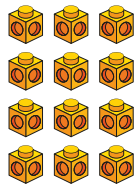
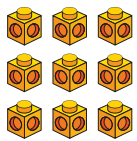
- Complete the number sentences to match the pictures.



Write  $>$  or  $<$  to complete the statement.

$6 \times 3 \bigcirc 6 \times 5$

- Complete the number sentences and write  $<$ ,  $>$  or  $=$  to compare the arrays.



$\underline{\quad} \times \underline{\quad} = \underline{\quad}$

$\underline{\quad} \times \underline{\quad} = \underline{\quad}$

- Write  $<$ ,  $>$  or  $=$  to complete the statement.

$2 \times 30 \bigcirc 4 \times 30$

- Write  $<$ ,  $>$  or  $=$  to compare the multiplications.

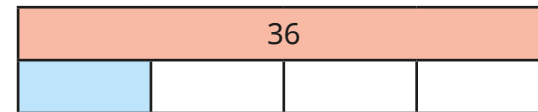
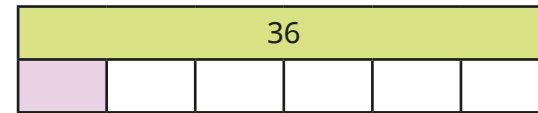
$8 \times 3 \bigcirc 7 \times 4$

$8 \times 2 \bigcirc 6 \times 4$

$80 \times 3 \bigcirc 70 \times 4$

$8 \times 20 \bigcirc 6 \times 40$

- How do the bar models show that  $36 \div 6 < 36 \div 4$ ?



Draw bar models to compare the pairs of calculations.

$12 \div 6 \bigcirc 12 \div 4$

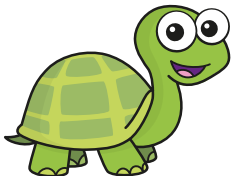
$15 \div 5 \bigcirc 15 \div 3$

$27 \div 3 \bigcirc 24 \div 3$

$20 \div 5 \bigcirc 20 \div 4$

# Reasoning about multiplication

## Reasoning and problem solving



$8 \times 8$   
is greater  
than double  
 $4 \times 8$

Do you agree with Tiny?  
Use counters to show your answer.

No  
 $8 \times 8 = \text{double } 4 \times 8$

Use all the cards to complete the statements.

$4 \times 5$	$3 \times 8$	$3 \times 4$
$5 \times 5$	$4 \times 8$	$3 \times 5$

\_\_\_\_\_ < \_\_\_\_\_  
 \_\_\_\_\_ > \_\_\_\_\_  
 \_\_\_\_\_ < \_\_\_\_\_

various possible answers, e.g.  
 $3 \times 5 < 4 \times 5$   
 $4 \times 8 > 3 \times 8$   
 $3 \times 4 < 5 \times 5$

Is each statement true or false?

$6 \times 7 < 6 + 6 + 6 + 6 + 6 + 6 + 6$

$7 \times 6 = 7 \times 3 + 7 \times 3$

$2 \times 3 > 5 \times 3$

False  
 True  
 False

Find three different ways to complete each number sentence.

\_\_\_\_\_  $\times 3 +$  \_\_\_\_\_  $\times 3 <$  \_\_\_\_\_  $\times 3$   
 \_\_\_\_\_  $\times 4 <$  \_\_\_\_\_  $\times 4 <$  \_\_\_\_\_  $\times 4$   
 \_\_\_\_\_  $\times 8 >$  \_\_\_\_\_  $\times 8 >$  \_\_\_\_\_  $\times 8$

multiple possible answers, e.g.  
 $1 \times 3 + 2 \times 3 < 5 \times 3$   
 $2 \times 4 < 8 \times 4 < 12 \times 4$   
 $7 \times 8 > 2 \times 8 > 1 \times 8$

# Multiply a 2-digit number by a 1-digit number – no exchange

## Notes and guidance

In this small step, children explore multiplying 2-digit numbers by 1-digit numbers. At this stage, none of the multiplication calculations require exchanges.

Children apply their understanding of partitioning to represent and solve calculations using the expanded method. The 2-digit number is partitioned into tens and ones, both are multiplied by the 1-digit number and then the partial products are added to find the total product. This is explored through a progression of representations from base 10 to place value counters and part-whole models, alongside number sentences.

The expanded method allows children to gain a deep understanding of the structure of the calculation before progressing to formal short multiplication in Year 4

### Things to look out for

- Children may partition a 2-digit number into single digits rather than tens and ones, for example  $48 \times 8 = 4 \times 8 + 8 \times 8$
- Errors may occur if partial products are lined up incorrectly.

## Key questions

- How can you partition a 2-digit number into tens and ones?
- What is the product of the tens and the single digit?
- What is the product of the ones and the single digit?
- What do you need to do to find the final answer?

## Possible sentence stems

- \_\_\_\_\_ tens and \_\_\_\_\_ ones multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_ tens multiplied by \_\_\_\_\_ and \_\_\_\_\_ ones multiplied by \_\_\_\_\_
- \_\_\_\_\_ tens multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_  
\_\_\_\_\_ ones multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_  
\_\_\_\_\_ multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_
- \_\_\_\_\_  $\times$  \_\_\_\_\_ = \_\_\_\_\_ tens  $\times$  \_\_\_\_\_ + \_\_\_\_\_  $\times$  \_\_\_\_\_

## National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

# Multiply a 2-digit number by a 1-digit number – no exchange

## Key learning

- Complete the number sentences.

Use the place value chart to help you.

Tens	Ones

$$3 \text{ tens} \times 2 = \text{ \_\_\_\_ } \text{ tens}$$

$$2 \text{ ones} \times 2 = \text{ \_\_\_\_ } \text{ ones}$$

$$\text{ \_\_\_\_ } + \text{ \_\_\_\_ } = \text{ \_\_\_\_ }$$

$$32 \times 2 = \text{ \_\_\_\_ }$$

- A minibus has space for 21 people.

How many people can fit on 3 minibuses?

Use a place value chart and base 10 to help you.

- Use the place value chart and counters to work out  $21 \times 4$

Tens	Ones

$$2 \text{ tens} \times 4 = \text{ \_\_\_\_ } \text{ tens}$$

$$1 \text{ one} \times 4 = \text{ \_\_\_\_ } \text{ ones}$$

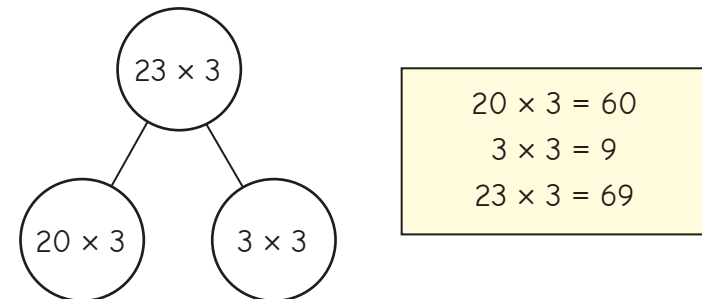
$$\text{ \_\_\_\_ } + \text{ \_\_\_\_ } = \text{ \_\_\_\_ }$$

$$21 \times 4 = \text{ \_\_\_\_ }$$

- Work out the multiplications.

$32 \times 3$	$23 \times 2$	$12 \times 4$	$41 \times 2$
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- Ron has used a part-whole model to multiply 23 by 3



Use a part-whole model to help you work out the multiplications.

$21 \times 5$	$42 \times 2$	$52 \times 2$	$21 \times 6$
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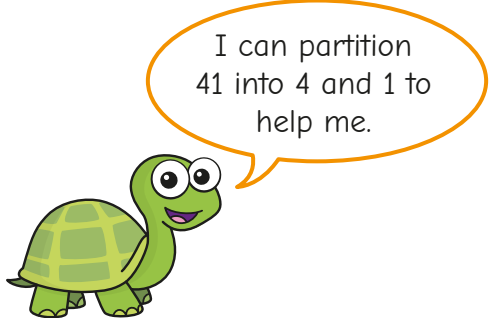
- Complete the number sentences.

<p>▶ <math>32 \times 4</math></p> <p>= ___ tens <math>\times</math> 4 + ___ ones <math>\times</math> 4</p> <p>= ___ + ___</p> <p>= ___</p>	<p>▶ <math>42 \times 3</math></p> <p>= ___ tens <math>\times</math> 3 + ___ ones <math>\times</math> 3</p> <p>= ___ + ___</p> <p>= ___</p>
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# Multiply a 2-digit number by a 1-digit number – no exchange

## Reasoning and problem solving

Tiny is working out  $41 \times 5$



I can partition 41 into 4 and 1 to help me.


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    graph TD
      A[41 x 5] --> B[4 x 5]
      A --> C[1 x 5]
      B --> D[20]
      C --> E[5]
      D --> F[25]
      E --> F
    
```

What has Tiny done wrong?  
Work out the correct answer.

205

Whitney is comparing calculations.




$4 \times 21 = 2 \times 42$

Is Whitney correct?  
How does she know this?

Yes

Ron multiplies a 2-digit number by a 1-digit number.



The answer is 48

What might Ron's numbers be?

48 and 1  
24 and 2  
12 and 4

# Multiply a 2-digit number by a 1-digit number – with exchange

## Notes and guidance

In this small step, children continue to explore multiplying 2-digit numbers by 1-digit numbers, now looking at calculations that involve an exchange.

As in the previous step, children apply their understanding of partitioning to represent and solve calculations using the expanded method. This involves partitioning the 2-digit number into tens and ones, multiplying separately, then adding the partial products together. Children use the same representations as in the previous steps to provide familiarity and focus their attention on the new aspect of making an exchange.

Use of the expanded method allows children to gain a deep understanding of the structure of the calculation before progressing to formal short multiplication in Year 4

### Things to look out for

- Children may partition a 2-digit number into single digits rather than tens and ones, for example  $48 \times 8 = 4 \times 8 + 8 \times 8$
- Children may not line up partial products correctly.
- Children may struggle when making an exchange, including forgetting to add on any exchanges.

## Key questions

- How can you partition a 2-digit number into tens and ones?
- What is the product of the tens and the single digit?
- What is the product of the ones and the single digit?
- What do you need to do to find the final answer?
- What do you do if you have ten or more ones?

## Possible sentence stems

- \_\_\_\_\_ tens and \_\_\_\_\_ ones multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_ tens multiplied by \_\_\_\_\_ and \_\_\_\_\_ ones multiplied by \_\_\_\_\_
- \_\_\_\_\_ ones is \_\_\_\_\_ tens and \_\_\_\_\_ ones.
- \_\_\_\_\_  $\times$  \_\_\_\_\_ = \_\_\_\_\_ tens  $\times$  \_\_\_\_\_ + \_\_\_\_\_  $\times$  \_\_\_\_\_

## National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods



# Multiply a 2-digit number by a 1-digit number – with exchange

## Key learning

- Complete the number sentences.

Use the place value chart to help you.

Tens	Ones

$2 \text{ tens} \times 4 = \underline{\quad\quad} \text{ tens}$   
 $4 \text{ ones} \times 4 = \underline{\quad\quad} \text{ ones}$   
 $24 \times 4 = \underline{\quad\quad} + \underline{\quad\quad} = \underline{\quad\quad}$   
 $24 \times 4 = \underline{\quad\quad}$

- Use the place value chart and counters to work out  $45 \times 3$

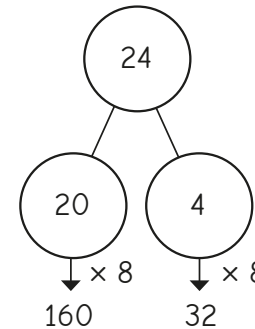
Tens	Ones

$4 \text{ tens} \times 3 = \underline{\quad\quad} \text{ tens}$   
 $5 \text{ ones} \times 3 = \underline{\quad\quad} \text{ ones}$   
 $\underline{\quad\quad} + \underline{\quad\quad} = \underline{\quad\quad}$   
 $45 \times 3 = \underline{\quad\quad}$

- Use a place value chart and base 10 to work out the multiplications.

$13 \times 4$	$23 \times 4$	$14 \times 8$	$25 \times 3$
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- Mo uses a part-whole model to work out  $24 \times 8$



$160 + 32 = 192$ $24 \times 8 = 192$
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Use Mo's method to work out the multiplications.

$18 \times 4$	$73 \times 5$	$42 \times 5$	$28 \times 8$
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- Complete the workings.

$\blacktriangleright 64 \times 3$   
 $= \underline{\quad} \text{ tens} \times 3 + \underline{\quad} \text{ ones} \times 3$   
 $= \underline{\quad} + \underline{\quad}$   
 $= \underline{\quad}$

$\blacktriangleright 24 \times 8$   
 $= 20 \times 8 + 4 \times 8$   
 $= \underline{\quad} + \underline{\quad}$   
 $= \underline{\quad}$

# Multiply a 2-digit number by a 1-digit number – with exchange

## Reasoning and problem solving

Is the statement always true, sometimes true or never true?



A 2-digit number multiplied by a 1-digit number has a 2-digit answer.

sometimes true

Explain your answer.



Aisha is sorting out two cupboards.



In the first cupboard, there are 4 boxes with 34 pencils in each box.  
In the second cupboard, there are 5 boxes with 28 pencils in each box.  
Which cupboard has more pencils?

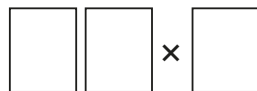
second cupboard

Here are some digit cards.



Use each digit card once to create a multiplication.

$23 \times 4 = 92$



Which multiplication gives an answer closest to 100?

Use the fact to compare the multiplications. Write < or > to make the statement correct.



$8 \times 44 = 352$

$8 \times 45$  ○  $9 \times 44$

<

How did the fact help you?



## Link multiplication and division

### Notes and guidance

In this small step, children develop their understanding of related facts from earlier in the block, with a focus on linking multiplication and division facts.

In particular, children explore what happens when a number within a calculation is multiplied by 10 and how this affects the answer. They use these facts by unitising in tens, for example using  $8 \div 2 = 4$  to derive  $8 \text{ tens} \div 2 = 4 \text{ tens}$ , so  $80 \div 2 = 40$ . A range of representations are used to make the link between multiples of one and ten, which will be familiar from the multiplication steps earlier in the block.

This step will support children to work out divisions in the next few steps of the block.

### Things to look out for

- Children may try to find results by calculation, rather than recognising the relationship between two facts.
- In examples such as  $240 \div 80$ , children may think the answer is 30 because they know  $24 \div 8 = 3$  and they assume that they need to add a zero.

### Key questions

- What is the same and what is different about the two calculations?
- How can you show the calculation using place value counters/ base 10?
- How is multiplying by 10s different from multiplying by 1s?
- What division facts do you know by using the fact  
\_\_\_\_\_  $\times$  \_\_\_\_\_ = \_\_\_\_\_?

### Possible sentence stems

- \_\_\_\_\_  $\times$  \_\_\_\_\_ ones is equal to \_\_\_\_\_ ones, so \_\_\_\_\_  $\times$  \_\_\_\_\_ tens is equal to \_\_\_\_\_ tens.
- \_\_\_\_\_  $\div$  \_\_\_\_\_ is equal to \_\_\_\_\_, so \_\_\_\_\_ tens  $\div$  \_\_\_\_\_ is equal to \_\_\_\_\_ tens.

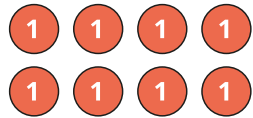
### National Curriculum links

- Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which  $n$  objects are connected to  $m$  objects

# Link multiplication and division

## Key learning

- What multiplication and division facts does the array show?



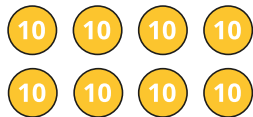
\_\_\_\_\_ × \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_ × \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_ ÷ \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_ ÷ \_\_\_\_\_ = \_\_\_\_\_

What multiplication and division facts does the array show?



\_\_\_\_\_ × \_\_\_\_\_ = \_\_\_\_\_

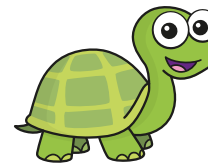
\_\_\_\_\_ × \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_ ÷ \_\_\_\_\_ = \_\_\_\_\_

\_\_\_\_\_ ÷ \_\_\_\_\_ = \_\_\_\_\_

What is the same and what is different about these arrays?

- Tiny is working out  $60 \div 3$



I know 6 ones  $\div$  3 is equal to 2 ones.  
So 6 tens  $\div$  3 is equal to 2 tens.  
 $60 \div 3 = 20$

Use Tiny's method to work out the divisions.

$80 \div 4$

$90 \div 3$

$60 \div 2$

$70 \div 7$

- Fill in the missing numbers.

$2 \times 6 = \underline{\quad}$        $3 \times 8 = \underline{\quad}$        $\underline{\quad} = 5 \times 3$

$2 \times 60 = \underline{\quad}$        $3 \times \underline{\quad} = 240$        $150 = 5 \times \underline{\quad}$

- 1 ticket to the zoo costs £20

How much do 4 tickets cost?

How many tickets can you buy for £180?

- There are 80 children in Year 3

The children are put into pairs.

How many pairs are there altogether?

# Link multiplication and division

## Reasoning and problem solving

Eight friends go to a theme park for the day.



- Tickets to the theme park cost £20 each.
- Lunch costs £10 each.

Four of the friends share the cost between them.

How much do they each pay?

£60

Write  $<$ ,  $>$  or  $=$  to compare the statements.

$8 \div 2$    $80 \div 2$

$80 \div 2$    $80 \div 4$

$60 \times 3$    $60 \div 3$

$4 \times 80$    $8 \times 40$

$<$   
 $>$   
 $>$   
 $=$

Work out the divisions.

$320 \div 2$	$320 \div 20$
$320 \div 4$	$320 \div 40$
$320 \div 8$	$320 \div 80$

160   16  
80   8  
40   4

What do you notice?



Amir is finding related calculations.



I know  $5 \times 8 = 40$ , so I also know all these other facts.

$5 \times 80 = 400$	$400 \div 5 = 80$
$50 \times 8 = 400$	$400 \div 8 = 50$

Which facts are correct?

They are all correct.

# Divide a 2-digit number by a 1-digit number – no exchange

## Notes and guidance

In this small step, children build on their knowledge of times-tables and division facts, using these to support them when dividing a 2-digit number by a 1-digit number. This step focuses on partitioning a number into tens and ones and sharing into equal groups, dividing numbers that do not involve exchanging or remainders. For example,  $63 \div 3$  can be partitioned into 60 and 3 and then shared into three equal groups:  $60 \div 3 = 20$  and  $3 \div 3 = 1$ , therefore  $63 \div 3 = 21$

Children use part-whole models and place value counters to represent the calculations and support their understanding. It is important that children divide the tens first and then the ones. While it would not have an impact on their answers in this particular step, getting used to dividing in this way is beneficial for when they move on to dividing numbers involving exchanging and remainders in future steps.

## Things to look out for

- Children may be used to working out a calculation starting with the ones column as this is what they have done with addition, subtraction and multiplication.
- Children may need support partitioning numbers into tens and ones.

## Key questions

- What is \_\_\_\_\_ partitioned into tens and ones?
- What is \_\_\_\_\_ shared into \_\_\_\_\_ equal groups?
- How can the place value counters help you divide \_\_\_\_\_ by \_\_\_\_\_?
- How can you use the part-whole model to work out the division?
- What is \_\_\_\_\_ divided by \_\_\_\_\_?

## Possible sentence stems

- \_\_\_\_\_ partitioned into tens and ones is \_\_\_\_\_ tens and \_\_\_\_\_ ones.
- \_\_\_\_\_ divided by \_\_\_\_\_ is equal to \_\_\_\_\_

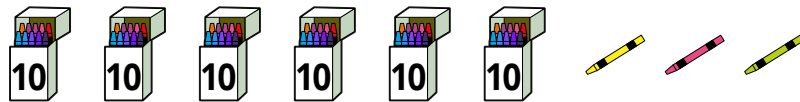
## National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

# Divide a 2-digit number by a 1-digit number – no exchange

## Key learning

- There are 63 crayons.



- Share the crayons into three equal groups.  
Use a place value chart and some counters to help you.
- Complete the sentences.

6 tens  $\div$  3 = \_\_\_\_\_ tens

3 ones  $\div$  3 = \_\_\_\_\_ one

63  $\div$  3 = \_\_\_\_\_

- Dani uses place value counters to work out  $39 \div 3$

Tens	Ones
10	1 1 1
10	1 1 1
10	1 1 1

$39 \div 3 = 13$

Use Dani's method to work out the divisions.

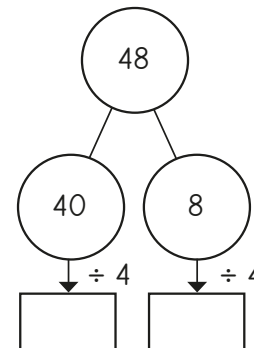
$84 \div 4$

$66 \div 2$

$66 \div 3$

$69 \div 3$

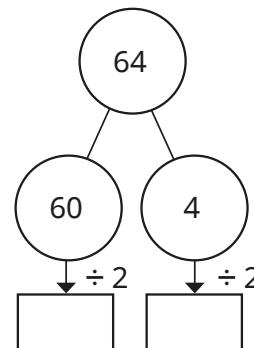
- Eva uses a part-whole model to work out  $48 \div 4$   
Complete Eva's workings.



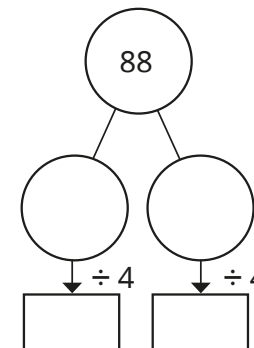
$48 \div 4 = \underline{\quad}$

- Work out the divisions.

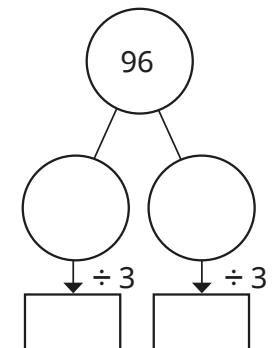
$64 \div 2 = \underline{\quad}$



$88 \div 4 = \underline{\quad}$



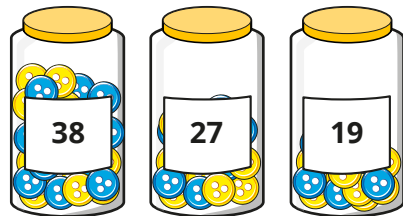
$96 \div 3 = \underline{\quad}$



# Divide a 2-digit number by a 1-digit number – no exchange

## Reasoning and problem solving

Tommy has 3 jars of buttons.



He shares all the buttons equally between 4 people.

How many buttons will each person get?

21

Write  $<$ ,  $>$  or  $=$  to compare the calculations.

$24 \div 2$  ○  $36 \div 3$

$84 \div 2$  ○  $84 \div 4$

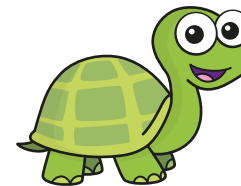
Explain your answers.

=

>

Tiny uses place value counters to work out  $44 \div 4$

Tens	Ones
10 10	1 1
10 10	1 1



The answer is 22

Is Tiny correct?

How do you know?

No

Huan thinks that 88 sweets can be shared equally between 8 people.

Is he correct?

How do you know?

Yes



# Divide a 2-digit number by a 1-digit number – flexible partitioning

## Notes and guidance

In this small step, children continue to divide a 2-digit number by a 1-digit number. They now begin to look at calculations that involve exchanging between the tens and the ones.

Children use their previous learning on flexible partitioning to support them with this. For example, to calculate  $42 \div 3$ , they need to identify multiples of 3 that 42 can be partitioned into. Children use their knowledge of times-tables facts to partition the number into multiples of the number they are dividing by. For this example, they can partition 42 into 30 and 12, and then use  $30 \div 3 = 10$  and  $12 \div 3 = 4$  to find that  $42 \div 3 = 14$

Children can use place value counters to support their understanding and part-whole models to show what calculations have been done.

## Things to look out for

- Children may be used to working out a calculation starting with the ones column as this is what they have done with addition, subtraction and multiplication.
- Children may not be confident with their times-table facts, which means they may find it difficult to partition the number into multiples of the number they are dividing by.

## Key questions

- How can you flexibly partition \_\_\_\_\_ so that the tens and ones are both multiples of the number you are dividing by?
- What is \_\_\_\_\_ shared into \_\_\_\_\_ equal groups?
- How can the place value counters help you divide \_\_\_\_\_ by \_\_\_\_\_?
- How can you use the part-whole model to work out the division?
- What is \_\_\_\_\_ divided by \_\_\_\_\_?

## Possible sentence stems

- \_\_\_\_\_ can be partitioned into \_\_\_\_\_ and \_\_\_\_\_, as these numbers are both multiples of \_\_\_\_\_
- \_\_\_\_\_ divided by \_\_\_\_\_ is equal to \_\_\_\_\_

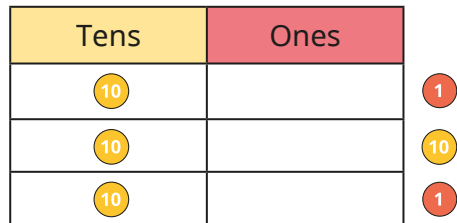
## National Curriculum links

- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

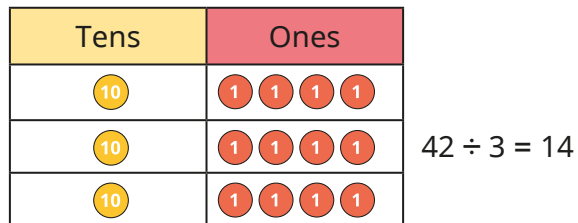
# Divide a 2-digit number by a 1-digit number – flexible partitioning

## Key learning

- Ron uses place value counters to work out  $42 \div 3$   
First, he shares the tens into 3 equal groups.  
He has 1 ten and 2 ones left over.



Ron exchanges the remaining ten for 10 ones.  
Then he shares the ones into 3 equal groups.



Use Ron's method to work out the divisions.

48 ÷ 3

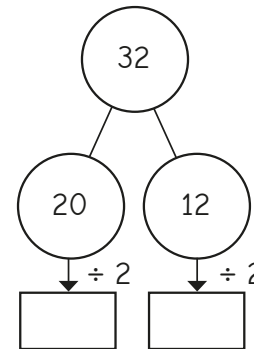
52 ÷ 4

65 ÷ 5

72 ÷ 6

- Use place value counters to divide 54 by 3  
What do you notice?

- Annie uses a part-whole model to work out  $32 \div 2$



$32 \div 2 = \underline{\quad}$

Why did Annie partition 30 into 20 and 12?  
Complete Annie's workings.

- Use part-whole models to work out the divisions.

$96 \div 4 = \underline{\quad}$

$96 \div 8 = \underline{\quad}$

$96 \div 6 = \underline{\quad}$

# Divide a 2-digit number by a 1-digit number – flexible partitioning

## Reasoning and problem solving

Jack is working out  $48 \div 3$



I can partition 48 into 40 and 8 to help me.

Is there a way to improve Jack's method?

partition 48 into 30 and 18, as these are both divisible by 3

Write  $<$ ,  $>$  or  $=$  to complete the statements.



$48 \div 4$    $45 \div 3$

$52 \div 4$    $42 \div 3$

$54 \div 3$    $60 \div 4$

$<$   
 $<$   
 $>$

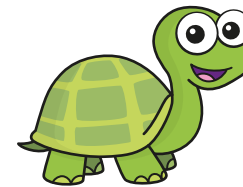
Did you need to work out all of the divisions?



Tiny uses the place value chart to work out  $54 \div 3$

Tens	Ones
10 10	1 1
10 10	1
10	1

18



The answer is 22

Explain the mistake Tiny has made.

Work out the correct answer.



# Divide a 2-digit number by a 1-digit number – with remainders

## Notes and guidance

In this small step, children continue to divide a 2-digit number by a 1-digit number. They apply their knowledge from the previous small steps and also make links between division and repeated subtraction, building on earlier learning.

Children look at calculations that may involve exchanging between the tens and ones, and that have a remainder. This will be the first time children have encountered remainders, so they will need to be explicitly taught the notation, for example  $43 \div 3 = 14$  remainder 1 or 14 r1

Practical equipment, such as lolly sticks and place value counters, can be used to support children's understanding.

## Things to look out for

- Children may be used to working out a calculation starting with the ones column, as this is what they have done with addition, subtraction and multiplication.
- Children may miscount when using repeated subtraction.
- Children may end up with a remainder that is greater than the number they are dividing by and need support to complete the calculation.

## Key questions

- Do you need to exchange any tens for ones?
- Is there a remainder?
- How can place value counters help you divide \_\_\_\_\_ by \_\_\_\_\_?
- How do you know \_\_\_\_\_ divided by \_\_\_\_\_ will have a remainder?
- Can a remainder ever be greater than the number you are dividing by?

## Possible sentence stems

- There are \_\_\_\_\_ groups of \_\_\_\_\_  
There are \_\_\_\_\_ remaining.  
So \_\_\_\_\_  $\div$  \_\_\_\_\_ = \_\_\_\_\_ r\_\_\_\_\_

## National Curriculum links

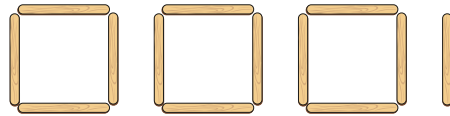
- Write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for 2-digit numbers times 1-digit numbers, using mental and progressing to formal written methods

# Divide a 2-digit number by a 1-digit number – with remainders

## Key learning

- Esther has 13 lolly sticks.

She uses them to make squares.



Complete the sentences.

There are \_\_\_\_\_ lolly sticks.

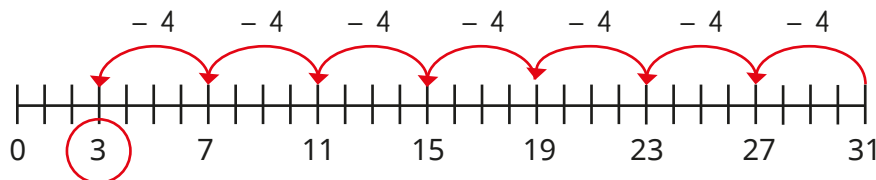
There are \_\_\_\_\_ groups of 4

There is \_\_\_\_\_ lolly stick remaining.

$13 \div 4 =$  \_\_\_\_\_ remainder \_\_\_\_\_

Esther can make \_\_\_\_\_ squares.

- Tommy uses repeated subtraction to work out  $31 \div 4$



$31 \div 4 = 7 \text{ r}3$

Use Tommy's method to work out  $38 \div 3$

- Alex uses place value counters to work out  $94 \div 4$   
First, she shares the tens into 4 equal groups.

Tens	Ones
10 10	
10 10	
10 10	
10 10	

She needs to exchange the remaining ten for 10 ones.

Alex shares as many of the ones as possible into 4 equal groups.

Tens	Ones
10 10	1 1 1
10 10	1 1 1
10 10	1 1 1
10 10	1 1 1

$94 \div 4 = 23 \text{ r}2$

Use Alex's method to work out the divisions.

$76 \div 3$

$62 \div 5$

$58 \div 4$

$83 \div 6$

# Divide a 2-digit number by a 1-digit number – with remainders

## Reasoning and problem solving

Which division is the odd one out?

$64 \div 8$	$77 \div 4$
$49 \div 6$	$65 \div 3$

How do you know?



various possible answers, e.g.  $64 \div 8$ , as it is the only calculation without a remainder

Tiny uses place value counters to work out  $68 \div 3$

Tens	Ones
10 10	1
10 10	1
10 10	1

1  
1  
1

Tiny's answer is 21 r5

What mistake has Tiny made?

Work out the correct answer.



22 r2

Teddy has some buttons.



- There are more than 30, but fewer than 50
- Teddy shares the buttons equally into 5 bowls. There is 1 button left over.
- Teddy shares the buttons equally into 4 bowls. There are no buttons left over.

How many buttons has Teddy got?

36

Dora and Tom are planting bulbs.



They have 76 bulbs altogether.

Dora plants her bulbs in rows of 8 and has 4 left over.

Tom plants his bulbs in rows of 10 and has 2 left over.

How many bulbs do they each have?

Dora: 44

Tom: 32

# Scaling

## Notes and guidance

In this small step, children develop their understanding of multiplication by focusing on scaling as opposed to repeated addition.

Building on concepts such as “3 times as many”, children use language such as “3 times the size of” when comparing, for example, lengths. It is important that children see this type of multiplication as well as repeated addition, as it will help them in their later study of ratio and scales. They can relate this to their knowledge of place value and understanding that the value of the column directly to the left of another is 10 times the value.

Bar models can be useful to represent the concept. String can be used to illustrate the idea of, for example, “twice as long as” and be related to a bar model representation.

## Things to look out for

- Children may not be familiar with models of multiplication other than those involving repeated addition.
- Children who are unfamiliar with the vocabulary may think that “3 times as many” means they need to add another three lots, resulting in a scale factor of 4 instead of 3

## Key questions

- What number is 10 times the size of \_\_\_\_\_?
- What number is \_\_\_\_\_ times the size of \_\_\_\_\_?
- What length is \_\_\_\_\_ times as long as \_\_\_\_\_?
- What time is \_\_\_\_\_ times as long as \_\_\_\_\_?
- Which is the larger object? How many times larger is it?
- How can you show the problem as a bar model?

## Possible sentence stems

- \_\_\_\_\_ is \_\_\_\_\_ times the length of \_\_\_\_\_
- \_\_\_\_\_ multiplied by \_\_\_\_\_ is equal to \_\_\_\_\_
- \_\_\_\_\_ times the size of \_\_\_\_\_ is \_\_\_\_\_

## National Curriculum links

- Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which  $n$  objects are connected to  $m$  objects

# Scaling

## Key learning

- Complete the sentences to describe the fruit.

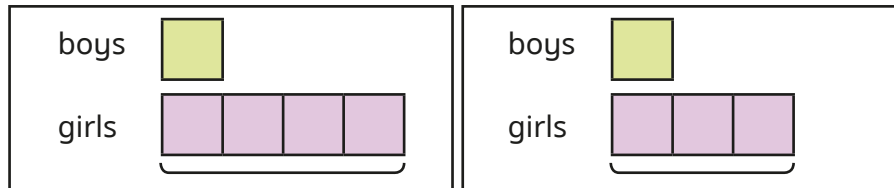


There are \_\_\_\_\_ bananas.

There are \_\_\_\_\_ strawberries.

There are \_\_\_\_\_ times as many strawberries as bananas.

- In a playground, there are 3 times as many girls as boys.



Which bar model shows the number of boys and girls?

Explain your choice.

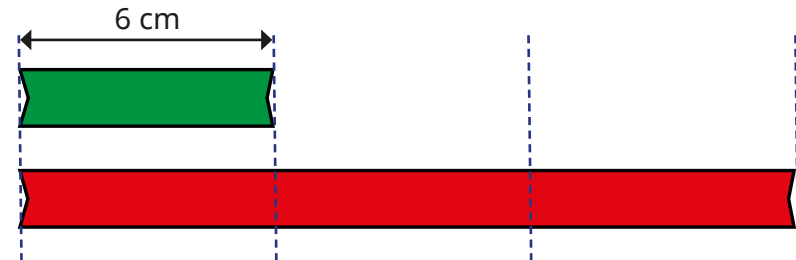
- Dexter has 2 pencils.

Kim has 5 times as many pencils as Dexter.

How many pencils has Kim got?

- The green ribbon is 6 cm long.

The red ribbon is 3 times as long as the green ribbon.



How long is the red ribbon?

Complete the number sentence.

$$6 \text{ cm} \times \underline{\quad} = \underline{\quad} \text{ cm}$$

- Rosie has a red pencil and a blue pencil.

The red pencil is 2 cm long.

The blue pencil is 4 times as long as the red pencil.

How long is the blue pencil?

- Whitney runs 25 m in 7 seconds.


Filip takes 5 times as long as Whitney to run 25 m.

How long does it take Filip to run 25 m?

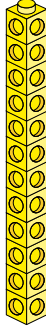


# Scaling


## Reasoning and problem solving

Mo and Eva build towers of cubes. 

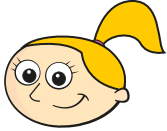
**Mo's tower**



**Eva's tower**




Mo's tower is 3 times as tall as my tower.




Eva


My tower is 12 times as tall as Eva's tower.



Mo

Who do you agree with?  
Explain your answer. 


Eva

Annie has some green and pink counters. 

- There are twice as many green counters as pink counters.
- There are 18 counters altogether.

How many green counters are there?

12

Dani, Amir and Jack are baking. 

- Dani needs 40 g of butter.
- Amir needs 3 times as much butter as Dani.
- Jack needs twice as much butter as Dani.

How much butter do they need altogether?

240 g

## How many ways?

### Notes and guidance

This small step focuses on correspondence problems.

Children start by systematically listing all the possible combinations resulting from combining two groups of objects. For example, if there are three buckets and four spades, children can explore how many different combinations of bucket and spade they can make.

The use of practical equipment to model a question can support children's understanding. Drawing a table helps children to take a systematic approach to ensure that they have found all the possible combinations. By the end of this step, children should be able to use multiplication to calculate the total number of possibilities, as a more efficient strategy than listing them all.

### Things to look out for

- When writing lists, unless working systematically, children may omit some possibilities and/or count some possibilities more than once.
- Children may not recognise the link between listing the number of possibilities and the multiplication calculation that can be done.

### Key questions

- How can you show the possibilities in a table?
- In what order should you list the possibilities?
- Starting with \_\_\_\_\_, how many combinations can you make?
- How do you know you have found all the ways?
- How many combinations are there if you have \_\_\_\_\_ and \_\_\_\_\_?

### Possible sentence stems

- For every \_\_\_\_\_, there are \_\_\_\_\_  
There are \_\_\_\_\_  $\times$  \_\_\_\_\_ = \_\_\_\_\_ possibilities altogether.
- For each \_\_\_\_\_, there are \_\_\_\_\_ choices of \_\_\_\_\_  
There are \_\_\_\_\_ ways altogether.
- I know that I have found them all because ...

### National Curriculum links

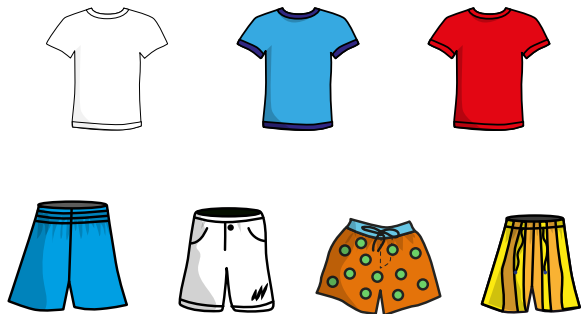
- Solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which  $n$  objects are connected to  $m$  objects

# How many ways?

## Key learning

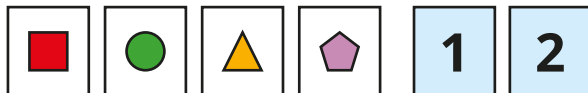
- Huan has three T-shirts and four pairs of shorts.

Complete the table to show how many different outfits he can make.



T-shirt	Shorts
white	blue
white	white
white	spotty
white	stripy

- Alex has four shape cards and two digit cards.



She chooses a shape and a digit.

Use a table to find all the different ways that she can do this.

How many different ways can you find?

How do you know that you have found them all?

- Ron has three hats and two scarves.



He chooses a hat and a scarf.

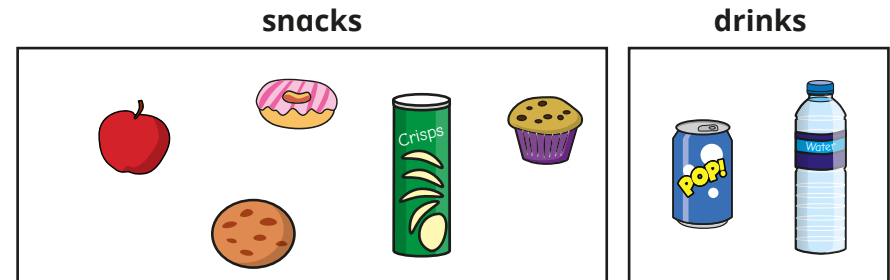
List all the possible combinations he can wear.

Use a multiplication to work out the number of combinations.

How many combinations are there if Ron buys four more scarves?

- Aisha is choosing a snack and a drink.

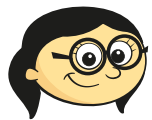
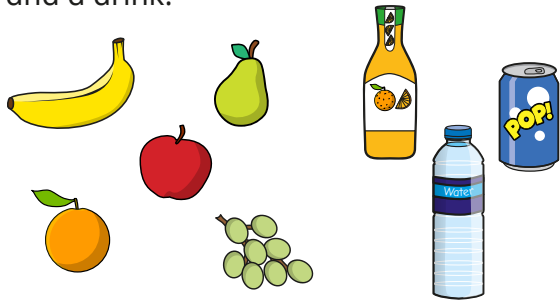
How many possible combinations are there?



# How many ways?

## Reasoning and problem solving

Annie chooses a piece of fruit and a drink.



There are 5 kinds of fruit and 3 drinks.  $5 + 3 = 8$ , so there are 8 possible combinations I could have.

Explain why Annie is wrong.

How many possible combinations are there altogether?

How many possible combinations include a bottle of drink?

15

10

Brett is choosing an ice cream.

He chooses one flavour of ice cream and one sauce.

There are 6 ice cream flavours.

There are 24 possible combinations of ice cream and sauce.

How many sauces are there?

4

Tommy has some jumpers and pairs of trousers.

He has more jumpers than pairs of trousers.

He can make 15 different outfits.

How many jumpers could he have?

How many pairs of trousers could he have?

Compare answers with a partner.

5 jumpers and 3 pairs of trousers

15 jumpers and 1 pair of trousers

Spring Block 2

# Length and perimeter

## Small steps

Step 1

Measure in metres and centimetres

Step 2

Measure in millimetres

Step 3

Measure in centimetres and millimetres

Step 4

Metres, centimetres and millimetres

Step 5

Equivalent lengths (metres and centimetres)

Step 6

Equivalent lengths (centimetres and millimetres)

Step 7

Compare lengths

Step 8

Add lengths

## Small steps

Step 9

Subtract lengths

Step 10

What is perimeter?

Step 11

Measure perimeter

Step 12

Calculate perimeter

# Measure in metres and centimetres

## Notes and guidance

In Year 2, children used either metres or centimetres to measure the length of objects. In this small step, they revise these skills, initially using a ruler to measure objects in centimetres. They then combine both units of measurement, such as 1 m and 20 cm, for example by measuring the lengths of desks or the heights of children in the class.

Children do not need to convert between metres and centimetres at this stage, and as they have not yet been introduced to decimals, lengths should remain in the format \_\_\_\_ m and \_\_\_\_ cm.

Provide opportunities for children to use different measuring equipment, including rulers, tape measures, metre sticks and trundle wheels.

## Things to look out for

- Children may measure from the end of the ruler or measuring tape rather than measuring from zero.
- When using more than one ruler to measure, children may place them end to end, rather than lining up zero with the end point of the previous ruler.
- Children may measure using the non-metric side of a ruler.

## Key questions

- Where should you start measuring from on your ruler?
- What is the length of \_\_\_\_ in centimetres?
- What is the length of \_\_\_\_ in metres?
- What is the length of \_\_\_\_ in metres and centimetres?
- Would you measure the length of the classroom in centimetres or metres? Why?
- What equipment would you use to measure the length of \_\_\_\_?

## Possible sentence stems

- The \_\_\_\_ is \_\_\_\_ cm long.
- The \_\_\_\_ is \_\_\_\_ m long.
- The \_\_\_\_ is \_\_\_\_ m and \_\_\_\_ cm long.

## National Curriculum links

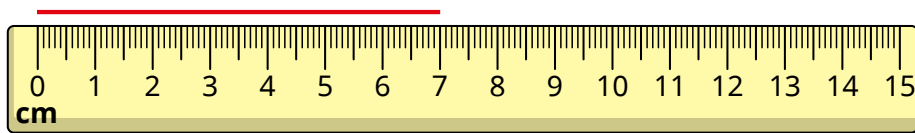
- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)



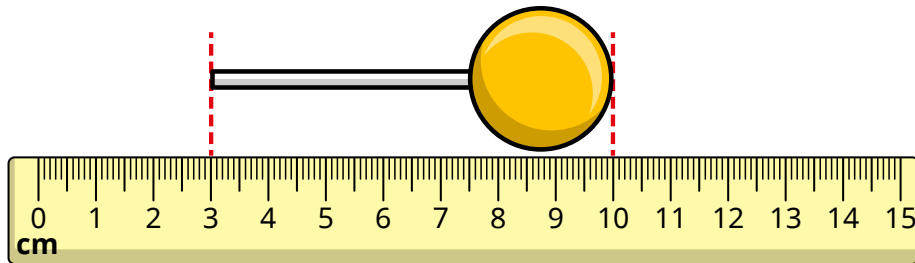
# Measure in metres and centimetres

## Key learning

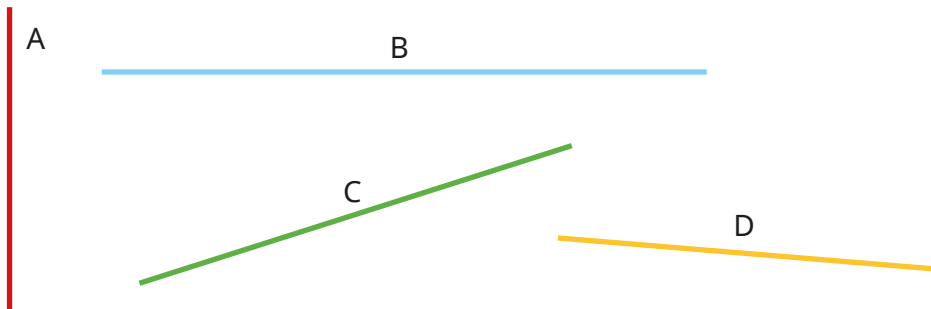
- What is the length of the line?



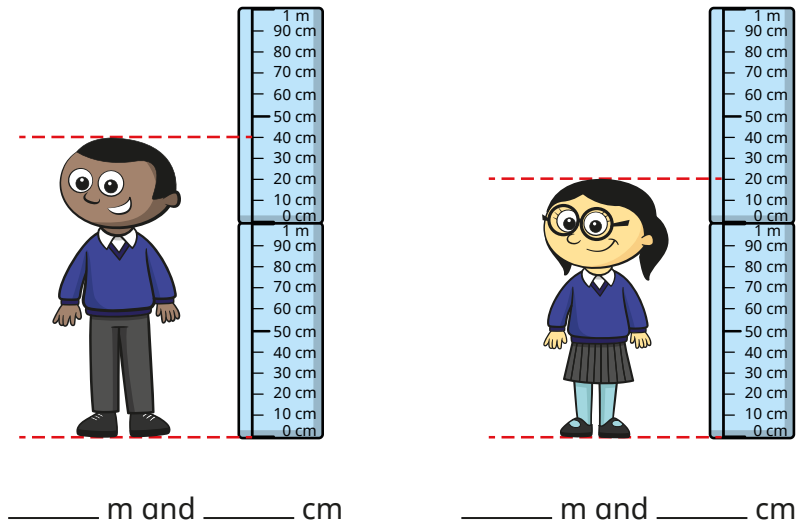
- What is the length of the lollipop?



- Use a ruler to measure the lines.



- Mo and Annie use metre sticks to measure their height. How tall are they?

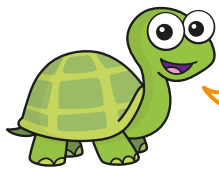


- Measure your classroom to complete the sentences.
  - The classroom is \_\_\_\_\_ m and \_\_\_\_\_ cm long.
  - The classroom is \_\_\_\_\_ m and \_\_\_\_\_ cm wide.
- ▶ Use a metre ruler to measure some other items in your classroom.
- ▶ Use a metre ruler to measure some items outside.

# Measure in metres and centimetres

## Reasoning and problem solving

Tiny is trying to measure the length of the line.



I cannot measure the line because my ruler is not long enough.

No

Do you agree with Tiny?

Why?



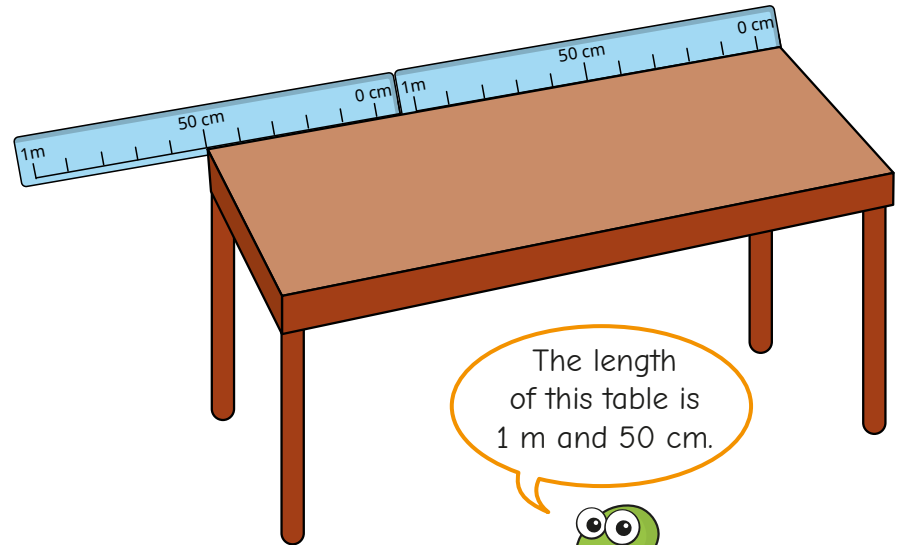
Dani draws a circle in chalk on the playground.

How could she measure the distance round the circle?

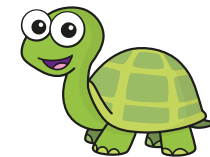


She could, for example, use a piece of string, wrap it round then measure the string.

Tiny is measuring the table top.



The length of this table is 1 m and 50 cm.



Do you agree with Tiny?

Explain your answer.



No

# Measure in millimetres

## Notes and guidance

This small step builds on children's understanding from the previous step by introducing millimetres as another unit of measurement.

Children need to understand that 1 mm is smaller than 1 cm and that millimetres can be used to measure lengths that are not an exact number of centimetres. Allow children time to explore a ruler with millimetre markings to see that there are 10 mm in 1 cm. Children could be encouraged to count in 10s and add on the remaining 1s when finding lengths. For example, when measuring a line that is 8 cm and 3 mm long, they can count in 10s to 80 mm and then add on the extra 3 mm to give a total length of 83 mm. However, at this stage children are not required to formally convert between centimetres and millimetres.

Children may find measuring oblique lines more difficult than horizontal or vertical lines. Model how rotating the page can make it easier to measure.

## Things to look out for

- Children may measure from the end of the ruler or measuring tape rather than measuring from zero.
- Children may give answers to the nearest centimetre rather than counting the millimetre intervals.

## Key questions

- Why is it important to start measuring from zero on your ruler?
- How many intervals are there between 0 and 1 cm? So how many millimetres are there in 1 cm?
- Where is the 5 mm mark on your ruler?
- What is the same and what is different about measuring a length in centimetres and measuring a length in millimetres?
- What is the length of \_\_\_\_\_ in millimetres?
- Would you measure the height of the door in millimetres?

## Possible sentence stems

- The \_\_\_\_\_ is \_\_\_\_\_ mm long.
- 1 mm is \_\_\_\_\_ than 1 cm.
- 1 mm is \_\_\_\_\_ than 1 m.

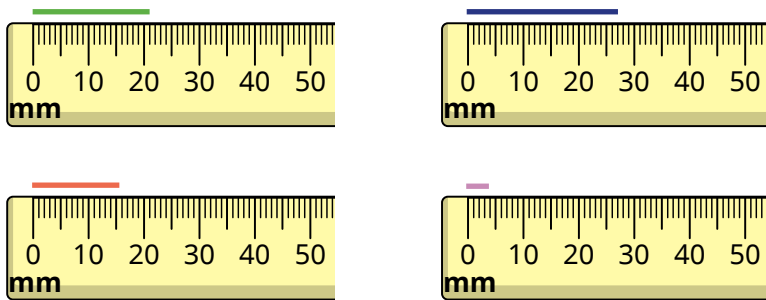
## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

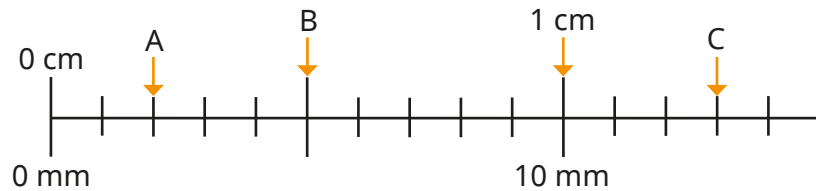
# Measure in millimetres

## Key learning

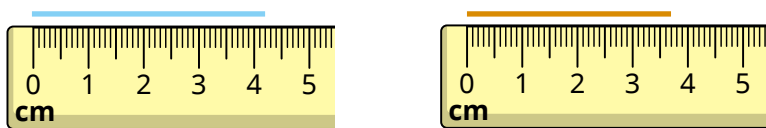
- What are the lengths of the lines in millimetres?



- What lengths are the arrows pointing to?



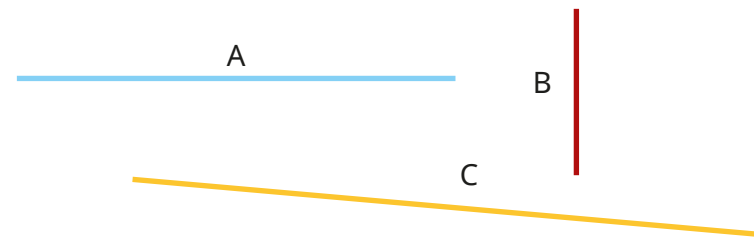
- What are the lengths of the lines in millimetres?



- Choose a phrase to complete each sentence.

less than      greater than

- ▶ 1 mm is \_\_\_\_\_ 1 cm.
- ▶ 1 m is \_\_\_\_\_ 1 mm.
- Measure these lines to the nearest millimetre.



- Find five things in your pencil case that you can measure in millimetres.

List them in order of size, starting with the smallest.

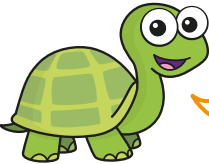
- Use a ruler to draw lines with these lengths.

- ▶ 80 mm      ▶ 25 mm      ▶ 51 mm
- ▶ 30 mm      ▶ 75 mm      ▶ 67 mm

# Measure in millimetres

## Reasoning and problem solving

Tiny is thinking about measuring a table.

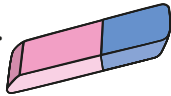



I cannot measure the table in millimetres, because it is too big.


Do you agree with Tiny?  
Explain your answer.

Tiny could measure the table in millimetres, but it is not the most efficient unit to use.

Whitney measures her rubber in millimetres.


My rubber is less than 60 mm. Its length is in the 5 times-table. The digits add up to 9




Work out the length of Whitney's rubber.

45 mm

Measure these two lines in millimetres.



Which line did you find easier to measure? Why?




lines measured accurately

Is the statement true or false?

A length measured in millimetres is always shorter than a length measured in centimetres.

Talk about it with a partner.



False

# Measure in centimetres and millimetres

## Notes and guidance

In this small step, children combine learning from the previous steps to measure objects in centimetres and millimetres. Measurements should be recorded in the form “4 cm and 3 mm”, and encourage children to record their measurements as centimetres and millimetres, not the other way around.

If possible, show children a ruler that has a centimetre scale on the top and a millimetre scale on the bottom to allow them to see the relationship between centimetres and millimetres.

If children are finding it difficult to measure using millimetre intervals, support them to identify the 5 mm interval on their ruler and count forwards or backwards. After sufficient practice, children’s measurements should be accurate to within 2 mm.

As well as measuring lengths, children also practise drawing lengths accurately.

## Things to look out for

- Children may inaccurately measure the millimetre part of a length, due to the intervals on the ruler being very close together.
- Children may record a length as, for example, 5 cm and 0 mm, rather than just 5 cm.

## Key questions

- Which is greater in length, 1 mm or 1 cm?
- What are the main things to remember in order to measure accurately using a ruler?
- Is the \_\_\_\_\_ an exact number of centimetres long?
- How many millimetres past the last centimetre interval does the \_\_\_\_\_ reach?
- How do you write a length that is not an exact number of centimetres?
- How does the 5 mm interval help you to measure the length?

## Possible sentence stems

- \_\_\_\_\_ cm \_\_\_\_\_ mm = \_\_\_\_\_ cm and \_\_\_\_\_ mm
- The \_\_\_\_\_ is \_\_\_\_\_ cm and \_\_\_\_\_ mm long.

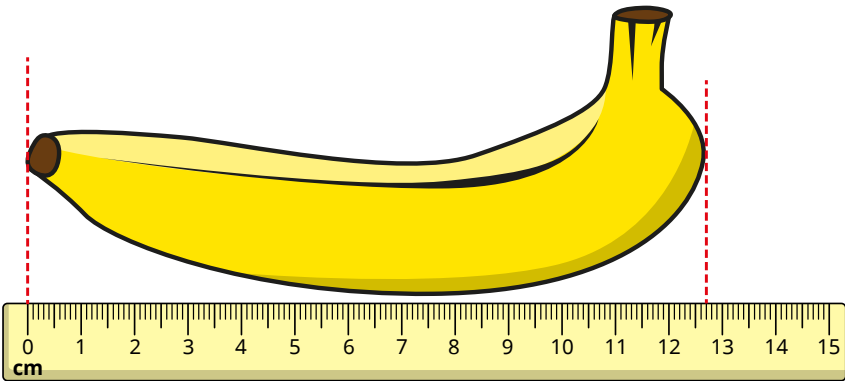
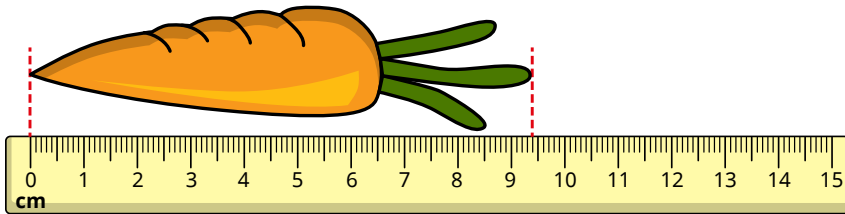
## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

# Measure in centimetres and millimetres

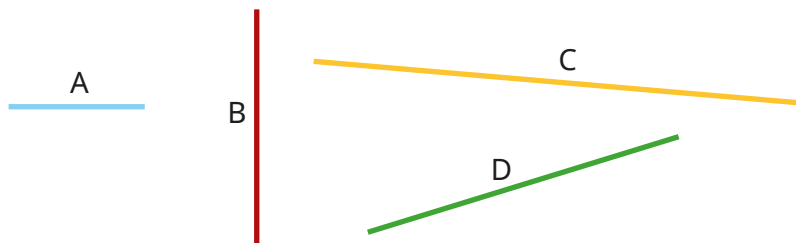
## Key learning

- What is the length of each object in centimetres and millimetres?



- Measure the lines.

Give your answers in centimetres and millimetres.



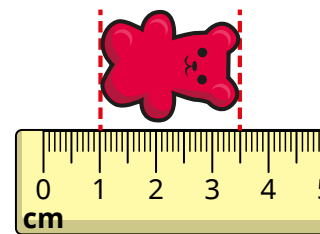
- Measure the length of some items in the classroom. Record the lengths in centimetres and millimetres. Compare answers with a partner. Are your answers exactly the same?

- Use a ruler to draw lines that measure:

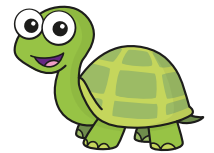
- between 4 cm and 5 cm
- between 65 mm and 80 mm
- between 10 mm and 2 cm
- between 3 cm 4 mm and 3 cm 9 mm

Ask a partner to measure and label each line.

- Tiny measures the sweet.



The sweet is 3 cm and 5 mm long.




Do you agree with Tiny?  
Explain your answer.

# Measure in centimetres and millimetres

## Reasoning and problem solving

Dexter, Alex and Tommy are comparing the lengths of their pencils.




**Dexter** says: My pencil is 15 cm.

**Alex** says: My pencil is half the length of Dexter's pencil.

**Tommy** says: My pencil is shorter than Dexter's pencil but longer than Alex's pencil.


What could be the length of Tommy's pencil?

Compare answers with a partner.



between 7 cm and 5 mm and 14 cm and 9 mm

Four children measure the height of a carton of juice.



**Teddy** says: It is 85 mm.

**Sam** says: It is 8 cm and 5 mm.


**Annie** says: It is 7 cm and 15 mm.

**Ron** says: It is 5 mm and 8 cm.

What is the same about their measurements?

What is different?

Talk about your answer with a partner.



All the children have given the same measurement, but they have expressed it differently.



# Metres, centimetres and millimetres

## Notes and guidance

In this small step, children compare and consider the appropriateness of different units of measurement.

Children need to understand that although, for example, metres are used to measure longer distances, it is still possible to measure these distances in centimetres or millimetres.

Encourage discussion about why it is important to choose the appropriate unit or measuring equipment before measuring an object or length.

Children make simple comparisons of lengths that do not require them to understand equivalent units of measurement, for example, comparing 3 m with 3 cm. By this stage, however, they should know how many centimetres are in 1 m and how many millimetres are in 1 cm.

## Things to look out for

- Children may focus on the number when comparing lengths, rather than considering the unit of measurement.
- Children may not have understood the relationship between millimetres, centimetres and metres.
- Children may need reminding of the meaning of the symbols  $<$ ,  $>$  and  $=$ .

## Key questions

- How many millimetres are there in a centimetre?
- How many centimetres are there in a metre?
- Which is longer, 1 m or 1 cm?
- Which is shorter, 1 cm or 1 mm?
- Which is longer, 3 m or 60 cm?
- Which is shorter, 4 cm or 20 mm?
- What unit would you use to measure the length of \_\_\_\_\_?

## Possible sentence stems

- \_\_\_\_\_ m is shorter/longer than \_\_\_\_\_ cm.
- \_\_\_\_\_ mm is shorter/longer than \_\_\_\_\_ cm.
- There are \_\_\_\_\_ mm in 1 cm.
- There are \_\_\_\_\_ cm in 1 m.

## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

# Metres, centimetres and millimetres

## Key learning

- Which unit would you use to measure each item?

Sort the items into the table.

length of a car	length of a pencil	
length of a fingernail	length of a garden	
length of a playground	height of a water bottle	
Metres	Centimetres	Millimetres

Compare answers with a partner.

- Write the lengths in order.

Start with the shortest length.

10 m	10 mm	10 cm
------	-------	-------

- Scott has 4 m of ribbon.

Aisha has 40 cm of ribbon.

Who has the longer piece of ribbon?

- Brett and Huan each draw a straight line.

Brett's line is 18 cm.

Huan's line is 30 mm.

Whose line is longer?

- Write  $<$ ,  $>$  or  $=$  to compare the lengths.

8 cm  10 mm

50 mm  2 m

14 m  98 cm

3 m and 87 cm  4 m

6 m and 20 cm  20 cm and 6 m

14 m and 5 cm  14 m and 5 mm

- Write the measurements in order.

Start with the longest measurement.

2 m	87 cm	3 cm	12 mm
-----	-------	------	-------

# Metres, centimetres and millimetres

## Reasoning and problem solving

Use the digit cards to complete the statement.



$$1 \text{ m and } 34 \text{ cm} < \boxed{\phantom{00}} \boxed{\phantom{00}} \boxed{\phantom{00}} \text{ cm} < 2 \text{ m}$$

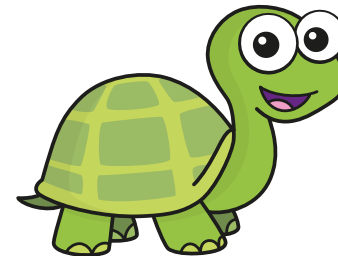
Find all the possible answers.

135 cm, 142 cm, 143 cm, 145 cm, 152 cm, 153 cm, 154 cm



Tiny is putting lengths in order.

I have put the lengths in order from shortest to longest.



13 mm, 29 cm, 1 m, 121 cm



What mistake has Tiny made?

Put the lengths in the correct order.



Is the statement always true, sometimes true or never true?

A length measured in metres will be longer than a length measured in centimetres.

Explain your answer.

sometimes true



## Equivalent lengths (metres and centimetres)

### Notes and guidance

In this small step, children use the fact that 1 m is equivalent to 100 cm. They use this to convert multiples of 100 cm into metres and metres into multiples of 100 cm. At the beginning of this step, it might be helpful to practise counting in 100s as a class.

Encourage children to partition the measurement into metres and centimetres when converting lengths that are not multiples of 100, for example  $134\text{ cm} = 1\text{ m and }34\text{ cm}$ . Part-whole models, bar models and double number lines are useful representations to support children in these conversions.

Children may also be encouraged to find and use common fractions to convert between metres and centimetres, for example  $\frac{1}{2}\text{ m}$  is equivalent to 50 cm, so  $4\frac{1}{2}\text{ m}$  is equivalent to 450 cm.

### Things to look out for

- Children may partition centimetres according to place value, which is inefficient when converting centimetres into metres. For example,  $163\text{ cm} = 100\text{ cm} + 60\text{ cm} + 3\text{ cm}$  rather than  $100\text{ cm} + 63\text{ cm}$ .
- When converting multiples of 100 cm, such as 400 cm, children may write 4 m and 0 cm.

### Key questions

- How many centimetres are there in 1 m?
- How can you work out how many centimetres there are in 6 m?
- What is \_\_\_\_\_ centimetres in metres?
- How many centimetres are there in \_\_\_\_\_ m and \_\_\_\_\_ cm?
- How can you partition 430 cm to help you to write the measurement in metres and centimetres?
- How many centimetres are there in  $\frac{1}{2}\text{ m}$ ?  
So how many centimetres are there in  $4\frac{1}{2}\text{ metres}$ ?

### Possible sentence stems

- There are \_\_\_\_\_ cm in 1 m.
- $1\text{ m} = 100\text{ cm}$ , so \_\_\_\_\_ m = \_\_\_\_\_ cm
- I can partition \_\_\_\_\_ cm into \_\_\_\_\_ cm and \_\_\_\_\_ cm.
- There are 100 cm in 1 m, so \_\_\_\_\_ cm = \_\_\_\_\_ m and \_\_\_\_\_ cm.
- $\frac{1}{2}\text{ m} =$  \_\_\_\_\_ cm

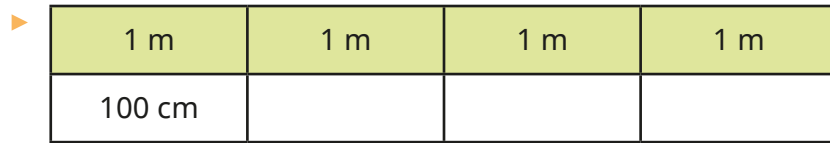
### National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

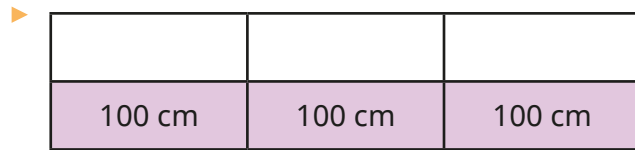
# Equivalent lengths (metres and centimetres)

## Key learning

- Use the bar models to complete the sentences.

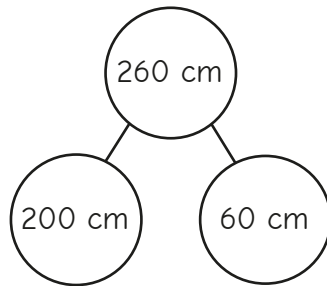


4 m = \_\_\_\_\_ cm



\_\_\_\_\_ m = 300 cm

- Esther uses the a part-whole model to find equivalent lengths.

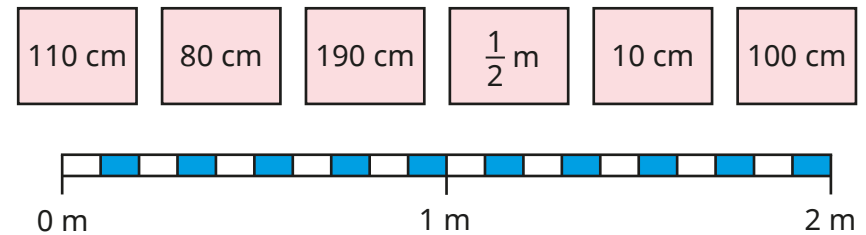


200 cm = 2 m  
260 cm = 2 m and 60 cm

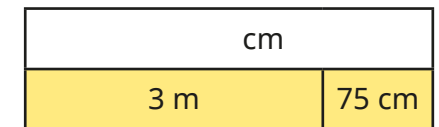
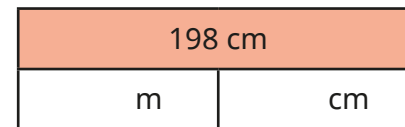
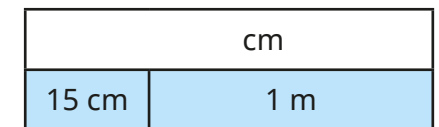
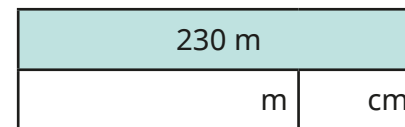
Use Esther's method to convert the lengths into metres and centimetres.

- |        |        |        |        |
|--------|--------|--------|--------|
| 120 cm | 125 cm | 367 cm | 542 cm |
|--------|--------|--------|--------|

- Where do the measurements belong on the measuring stick?



- Complete the bar models.



- Complete the sentences.
  - ▶ 3 m and 52 cm = \_\_\_\_\_ cm
  - ▶ 2 m and 19 cm = \_\_\_\_\_ cm
  - ▶ 483 cm = \_\_\_\_\_ m and \_\_\_\_\_ cm
  - ▶ 501 cm = \_\_\_\_\_ m and \_\_\_\_\_ cm

# Equivalent lengths (metres and centimetres)

## Reasoning and problem solving

Is the statement true or false?

$$413 \text{ cm} > 4 \text{ m and } 31 \text{ cm}$$

False

Explain your answer.



Which measurement is the odd one out?

250 cm

25 cm

$2\frac{1}{2}$  m

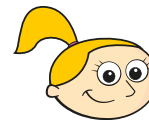
2 m 50 cm

25 cm

Explain your choice.



Eva and Jack each have a skipping rope.



Eva

I have the longer skipping rope.  
My skipping rope is  $2\frac{1}{2}$  m long.

My skipping rope is 220 cm. It is longer than Eva's because 220 is greater than  $2\frac{1}{2}$



Jack

Eva

Her skipping rope is 250 cm long, which is 30 cm longer than 220 cm.

Who is correct?

Explain your answer.

## Equivalent lengths (centimetres and millimetres)

### Notes and guidance

In this small step, children use the fact that 1 cm is equivalent to 10 mm. They use this to convert millimetres into centimetres and centimetres into millimetres. Recapping previous knowledge of multiples of 10 from Spring Block 1 may be useful prior to teaching this new content.

As children have not yet formally explored multiplying and dividing by 10, they should be encouraged to partition measurements into centimetres and millimetres when converting lengths that are not multiples of 10, for example  $34 \text{ mm} = 30 \text{ mm} + 4 \text{ mm} = 3 \text{ cm and } 4 \text{ mm}$ .

As in previous steps, children do not need to use decimal notation in this step. Bar models, part-whole models and double number lines are also useful representations to explore the connection between units of measurement.

### Things to look out for

- Once a length has been partitioned, children may convert the incorrect part, for example  $52 \text{ mm} = 2 \text{ cm and } 5 \text{ mm}$ .
- Children may convert centimetres to millimetres, but then forget to add on the remaining millimetres, for example  $6 \text{ cm } 7 \text{ mm} = 60 \text{ mm}$ .

### Key questions

- How many millimetres are there in 1 cm?
- How can you work out how many millimetres there are in 4 cm?
- How many millimetres are there in \_\_\_\_\_ cm and \_\_\_\_\_ mm?
- How do you know \_\_\_\_\_ mm and \_\_\_\_\_ cm are equivalent?
- How can you partition 47 mm to help you convert into centimetres and millimetres?
- How many millimetres are there in  $\frac{1}{2}$  cm?

### Possible sentence stems

- 1 cm = 10 mm, so \_\_\_\_\_ mm = \_\_\_\_\_ cm
- 1 cm = 10 mm, so \_\_\_\_\_ cm = \_\_\_\_\_ mm
- \_\_\_\_\_ mm = \_\_\_\_\_ mm + \_\_\_\_\_ mm = \_\_\_\_\_ cm and \_\_\_\_\_ mm
- \_\_\_\_\_ cm and \_\_\_\_\_ mm = \_\_\_\_\_ mm + \_\_\_\_\_ mm = \_\_\_\_\_ mm

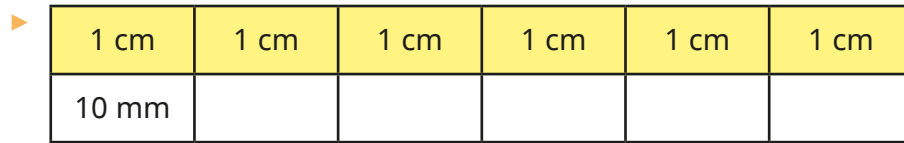
### National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

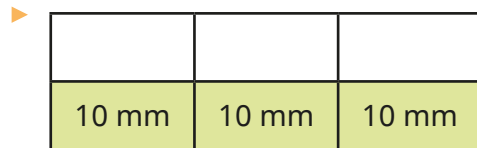
# Equivalent lengths (centimetres and millimetres)

## Key learning

- Use the bar models to complete the sentences.



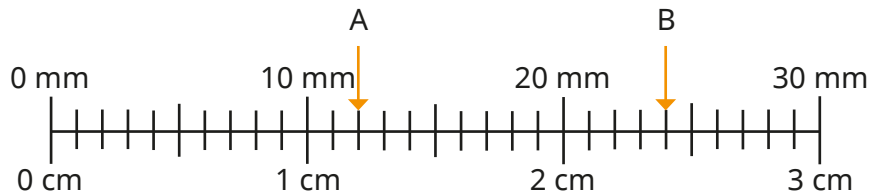
6 cm = \_\_\_\_\_ mm



30 mm = \_\_\_\_\_ cm

- What measurements are the arrows pointing to?

Complete the sentences.



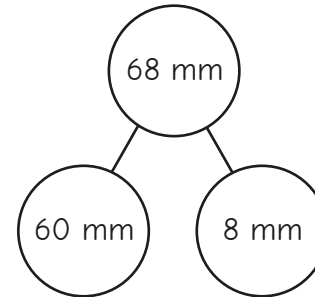
▶ A = \_\_\_\_\_ cm and \_\_\_\_\_ mm

A = \_\_\_\_\_ mm

▶ B = \_\_\_\_\_ cm and \_\_\_\_\_ mm

B = \_\_\_\_\_ mm

- Whitney uses a part-whole model to find an equivalent length.

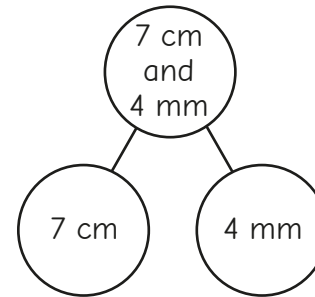


60 mm = 6 cm  
68 mm = 6 cm and 8 mm

Use Whitney's method to convert the lengths into centimetres and millimetres.

- ▶ 24 mm      ▶ 35 mm      ▶ 91 mm      ▶ 88 mm

- Ron uses a part-whole model to find an equivalent length.



7 cm = 70 mm  
7 cm and 4 mm = 74 mm

Use Ron's method to convert the lengths into millimetres.

- ▶ 6 cm and 8 mm      ▶ 8 cm and 6 mm      ▶ 1 cm and 9 mm



# Equivalent lengths (centimetres and millimetres)

## Reasoning and problem solving

Mo, Rosie and Kim are finding equivalent lengths.



40 cm and 7 mm is equivalent to 47 mm.

Mo



4 cm and 7 mm is equivalent to 47 mm.

Rosie



7 mm and 4 cm is equivalent to 47 mm.

Kim

Whose conversion is incorrect?

Whose conversion could be improved?

Talk about your answers with a partner.



Mo

Kim

Dexter is thinking of a measurement.



In millimetres, my measurement is a multiple of 2. It is greater than 81 mm. It can be partitioned as 8 cm and \_\_\_\_\_ mm.

82 mm, 84 mm, 86 mm or 88 mm

What measurement could Dexter be thinking of?

Which measurement is the odd one out?

500 mm	50 cm
$\frac{1}{2}$ m	500 cm

500 cm

Explain your choice.



# Compare lengths

## Notes and guidance

In this small step, children compare and order lengths using comparison language and inequality symbols. Building on the previous two steps, they need to convert all the measurements to the same unit of length before comparing.

Children can use practical equipment to justify decisions, measuring and comparing lengths of objects inside and outside the classroom to practise their measuring skills.

Children may need reminding of the meaning of the inequality symbols,  $<$  and  $>$ . Recapping how many millimetres are in a centimetre and how many centimetres are in a metre will also be useful.

Ensure children are aware that while they use the words shorter/longer when comparing lengths, they should use shorter/taller when talking about height.

## Things to look out for

- If children attempt to compare lengths without converting into the same unit of measurement, they may make mistakes.
- Children need very secure place value understanding when comparing a length in metres with a length in millimetres.

## Key questions

- How can you compare lengths given in different units?
- Why does finding equivalent lengths with the same unit make it easier to compare lengths?
- Does it matter which unit of measurement you use to compare?
- Is the unit of measurement or the size of the number more important?
- How many mm/cm are there in \_\_\_\_\_ cm/m?

## Possible sentence stems

- \_\_\_\_\_ m \_\_\_\_\_ cm is equal to \_\_\_\_\_ cm.
- \_\_\_\_\_ cm is \_\_\_\_\_ than \_\_\_\_\_ cm, so the greater length is \_\_\_\_\_ cm.
- \_\_\_\_\_ cm is equal to \_\_\_\_\_ mm.
- \_\_\_\_\_ mm is \_\_\_\_\_ than \_\_\_\_\_ mm, so the greater length is \_\_\_\_\_ mm.

## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

# Compare lengths

## Key learning

- Jack is comparing 34 mm and 3 cm 6 mm.

Complete the sentences.

- ▶ 3 cm 6 mm = \_\_\_\_\_ mm
- ▶ 34 mm is \_\_\_\_\_ than \_\_\_\_\_ mm.

Is there another way to compare the measurements?

- Amir and Dora measure their heights.
  - Amir's height is 127 cm.
  - Dora's height is 1 m and 30 cm.

Write **taller** or **shorter** to complete the sentences.

- ▶ Amir is \_\_\_\_\_ than Dora.
- ▶ Dora is \_\_\_\_\_ than Amir.

- Write <, > or = to compare the lengths.

101 cm ○ 1 m 10 cm

80 mm ○ 8 cm

90 cm ○ 90 mm

500 mm ○ 1 m 50 cm

- Write the lengths in order.

Start with the shortest length.

230 cm	750 mm	2 m 25 cm
2 m	1 m 75 cm	170 cm

- Fill in the missing numbers to make the statements correct.
  - ▶ 4 cm < \_\_\_\_\_ mm
  - ▶ \_\_\_\_\_ m < 378 cm
  - ▶ 245 mm = \_\_\_\_\_ cm + \_\_\_\_\_ mm
  - ▶ 5 m > \_\_\_\_\_ m and 99 cm
- Four friends are building towers.
  - Filip's tower is 22 cm and 7 mm tall.
  - Tom's tower is 22 cm tall.
  - Nijah's tower is 215 mm tall.
  - Dani's tower is 260 mm tall.

Complete the statement to put the towers in height order.

\_\_\_\_\_ < \_\_\_\_\_ < \_\_\_\_\_ < \_\_\_\_\_

# Compare lengths

## Reasoning and problem solving

Brett has put some lengths in order from shortest to longest.



170 mm

74 cm 7 mm

$1\frac{1}{2}$  m

Fill in the missing measurement.

Find three possible answers.



between  
74 cm 8 mm and  
1 m 49 cm

Sort the lengths into the table.

1 m 65 cm

165 mm

165 m

165 cm

160 cm 5 mm

16 cm 5 mm

Longer than a metre	Shorter than a metre

Are any of the lengths equivalent?

longer than a metre:  
1 m 65 cm, 165 m,  
165 cm,  
160 cm 5 mm

shorter than a metre:  
165 mm,  
16 cm 5 mm

equivalent lengths:  
1 m 65 cm and  
165 cm  
165 mm and  
16 cm 5 mm

# Add lengths

## Notes and guidance

In this small step, children add lengths. They begin by adding lengths that are measured in the same unit of measurement, before adding lengths that have different units.

When measurements have different units, children should find equivalent lengths with the same unit to allow them to add the two lengths. It is important to explore with children that this can be done in two ways, for example  $38\text{ mm} + 2\text{ cm}$  could be added as  $38\text{ mm} + 20\text{ mm}$  or as  $3\text{ cm} + 8\text{ mm} + 2\text{ cm} + 1\text{ mm}$ . Encourage children to discuss the different strategies available when adding lengths, before choosing the most efficient method.

This step provides an opportunity to revisit addition both with and without exchanges as covered in Autumn Block 2

Children will use skills learnt in this step when adding lengths to find the perimeter later in the block.

## Things to look out for

- If children are not secure with converting units of measurement, they may make errors when adding lengths.
- Children may add lengths without converting the units of measurement, for example  $14\text{ cm} + 24\text{ mm} = 38\text{ cm}$ .

## Key questions

- How many centimetres are there in 1 m?
- How many millimetres are there in 1 cm?
- Why is it important the lengths have the same unit of measurement before adding them?
- Which unit of measurement will you use to find equivalent lengths before adding them? Why?
- How did you find the total length?
- Does it matter in which order you add the lengths?

## Possible sentence stems

- \_\_\_\_\_ cm + \_\_\_\_\_ mm = \_\_\_\_\_ mm + \_\_\_\_\_ mm = \_\_\_\_\_ mm
- \_\_\_\_\_ m + \_\_\_\_\_ cm = \_\_\_\_\_ cm + \_\_\_\_\_ cm = \_\_\_\_\_ cm
- I am going to convert all of the units of measurement to \_\_\_\_\_ because ...

## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)

# Add lengths

## Key learning

- Dora builds this tower out of boxes.

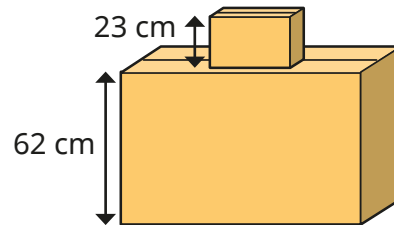
▶ How tall is Dora's tower?

Dora puts a third box on the tower.

The box is 30 cm tall.

▶ How tall is Dora's tower now?

Can you write your answer another way?



- Teddy and Kim are working out  $350 \text{ cm} + 1 \text{ m } 20 \text{ cm}$ .

### Teddy's method

$$350 \text{ cm} + 1 \text{ m } 20 \text{ cm}$$

$$350 \text{ cm} + 120 \text{ cm} = 470 \text{ cm}$$

### Kim's method

$$350 \text{ cm} + 1 \text{ m } 20 \text{ cm}$$

$$3 \text{ m } 50 \text{ cm} + 1 \text{ m } 20 \text{ cm}$$

$$3 \text{ m} + 1 \text{ m} = 4 \text{ m}$$

$$50 \text{ cm} + 20 \text{ cm} = 70 \text{ cm}$$

$$4 \text{ m and } 70 \text{ cm}$$

Talk about their methods with a partner.

Use both methods to work out the additions.

$$3 \text{ m } 65 \text{ cm} + 240 \text{ cm}$$

$$135 \text{ cm} + 5 \text{ m and } 20 \text{ cm}$$

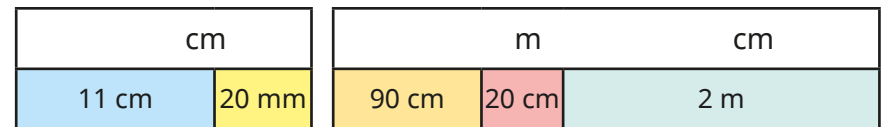
- Complete the additions.

▶  $7 \text{ cm} + 30 \text{ mm} = 7 \text{ cm} + \underline{\hspace{1cm}} \text{ cm} = \underline{\hspace{1cm}} \text{ cm}$

▶  $22 \text{ mm} + 4 \text{ cm} = 22 \text{ mm} + \underline{\hspace{1cm}} \text{ mm} = \underline{\hspace{1cm}} \text{ mm}$

▶  $\underline{\hspace{1cm}} \text{ cm} = \frac{1}{2} \text{ m} + 28 \text{ cm}$

- Complete the bar models.



- Sam, Ron and Esther take part in a standing jump competition.

Complete the table to show their total jump distances.

Child	Jump 1	Jump 2	Jump 3	Total
Sam	90 cm	65 cm	1 m 10 cm	
Ron	85 cm	85 cm	80 cm	
Esther	75 cm	1 m	1 m 25 cm	

Who jumped the greatest total distance?

# Add lengths

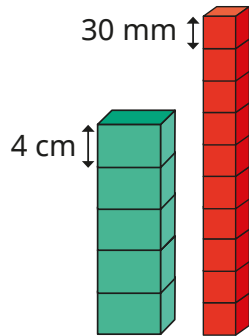
## Reasoning and problem solving

Red cubes are 30 mm tall.  
Green cuboids are 4 cm tall.

Tommy builds these towers.

Work out the height of each tower.

Give your answer in centimetres and in millimetres.



How much taller is the red tower than the green tower?

Draw a tower of red cubes that is between 12 cm and 24 cm tall.

Draw a tower of green cuboids that is between 12 cm and 24 cm tall.

How many answers can you find?

green tower:  
20 cm, 200 mm

red tower:  
30 cm, 300 mm

10 cm, 100 mm

4 to 8 red cubes

3 to 6 green cuboids

Work out the missing length.

$$234 \text{ cm} + 1 \text{ m } 83 \text{ cm} = 2 \text{ m} + \square \text{ cm}$$

217 cm

Compare methods with a partner.

Which is the odd one out?

$$4 \text{ m} + 30 \text{ cm} + 70 \text{ cm}$$

$$245 \text{ cm} + 255 \text{ cm}$$

$$50 \text{ mm} + 4 \text{ m} + 95 \text{ cm}$$

$$3\frac{1}{2} \text{ m} + 1\frac{1}{2} \text{ m}$$

All calculations add up to 5 m.

Possible answers may refer to units of measurement, fractions, number of digits.

Explain your choice.

# Subtract lengths

## Notes and guidance

In this small step, children begin by subtracting lengths that are measured in the same unit of measurement. They then look at subtracting millimetres from a whole number of centimetres as well as centimetres from a whole number of metres using simple conversions, for example  $1\text{ m} - 35\text{ cm}$  and  $4\text{ cm} - 3\text{ mm}$ . They then explore more complex examples where the lengths have different units of measurement and therefore equivalent lengths need to be found, for example  $4\text{ m } 36\text{ cm} - 112\text{ cm}$ . This can be a useful opportunity to also revisit subtraction where there is a need for exchange, for example  $2\text{ m } 43\text{ cm} - 118\text{ cm}$ .

Children should be exposed to the different structures of subtraction through word problems: partitioning, reduction and difference. Bar models can be a useful pictorial representation to highlight these different structures.

### Things to look out for

- If children are not secure with converting between units of measurement, they may make errors when subtracting lengths.
- Children may subtract lengths without converting the units of measurement, for example  $71\text{ cm} - 5\text{ mm} = 66\text{ cm}$ .

## Key questions

- How many centimetres are there in \_\_\_\_\_ m and \_\_\_\_\_ cm?
- Why is it important that the lengths have the same unit of measurement before you subtract them?
- Which unit of measurement will you use to find equivalent lengths before you subtract them? Why?
- What is the difference in length between the two objects?
- How can you check that you have the correct answer?

## Possible sentence stems

- \_\_\_\_\_ mm/cm = 1 cm/1 m
- \_\_\_\_\_ cm – \_\_\_\_\_ mm = \_\_\_\_\_ mm – \_\_\_\_\_ mm = \_\_\_\_\_ mm
- \_\_\_\_\_ m – \_\_\_\_\_ cm = \_\_\_\_\_ cm – \_\_\_\_\_ cm = \_\_\_\_\_ cm
- I am going to convert all of the units of measurement to \_\_\_\_\_ because ...

## National Curriculum links

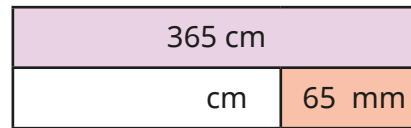
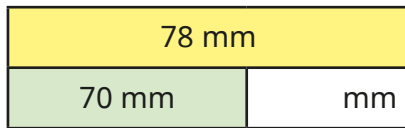
- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)



# Subtract lengths

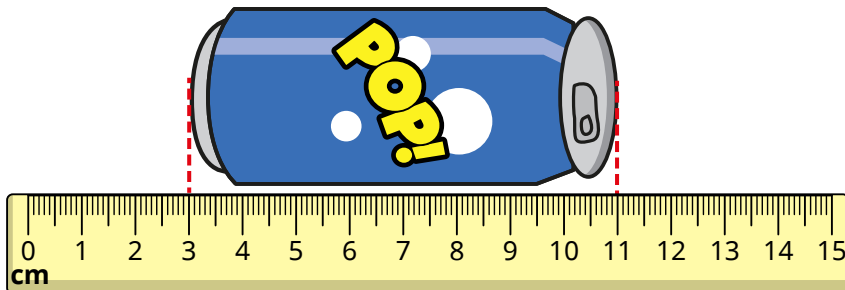
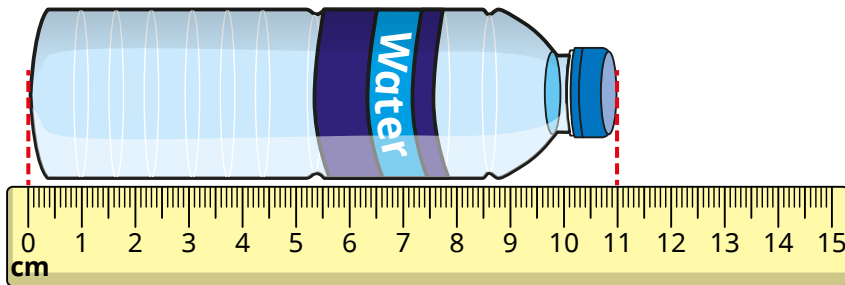
## Key learning

- Complete the bar models.



- What is the difference in length between the bottle of water and the can of fizzy drink?

Write your answer in centimetres.



- Complete the subtractions.

▶  $1\text{ m} - 42\text{ cm} = \underline{\hspace{2cm}}\text{ cm}$                       ▶  $5\text{ cm} - 3\text{ mm} = \underline{\hspace{2cm}}\text{ mm}$   
 ▶  $3\text{ m} - 42\text{ cm} = \underline{\hspace{1cm}}\text{ m } \underline{\hspace{1cm}}\text{ cm}$             ▶  $88\text{ mm} = 10\text{ cm} - \underline{\hspace{2cm}}\text{ mm}$

- Tommy and Eva are working out  $3\text{ m } 85\text{ cm} - 120\text{ cm}$ . Here are their workings.

### Tommy's method

$$\begin{aligned}
 3\text{ m } 85\text{ cm} - 120\text{ cm} \\
 120\text{ cm} = 1\text{ m } 20\text{ cm} \\
 3\text{ m} - 1\text{ m} = 2\text{ m} \\
 85\text{ cm} - 20\text{ cm} = 65\text{ cm} \\
 3\text{ m } 85\text{ cm} - 120\text{ cm} = 2\text{ m } 65\text{ cm}
 \end{aligned}$$

### Eva's method

$$\begin{aligned}
 3\text{ m } 85\text{ cm} - 120\text{ cm} \\
 3\text{ m} = 300\text{ cm} \\
 3\text{ m } 85\text{ cm} = 385\text{ cm} \\
 385\text{ cm} - 120\text{ cm} = 265\text{ cm} \\
 3\text{ m } 85\text{ cm} - 120\text{ cm} = 265\text{ cm}
 \end{aligned}$$

Whose method do you prefer?

- Kim has 5 m of rope. She uses 1 m and 54 cm to make a skipping rope. How much rope does she have left?

# Subtract lengths

## Reasoning and problem solving

A bike race is 950 m long.

Dora cycles 243 m and stops for a break.

She cycles another 459 m and stops for another break.

How much further does she need to cycle to complete the race?



248 m

A train engine is 20 metres long.

A car is  $15\frac{1}{2}$  m shorter than the train.

A bike is 250 cm shorter than the car.

Work out the length of the car.

Work out the length of the bike.

How much longer is the train than the bike?



$4\frac{1}{2}$  m

200 cm or 2 m

18 m

Tom has a 3 m roll of ribbon.

He is cutting it up into 10 cm lengths.

How many lengths can he cut?



30

60 cm, 6 lengths

Tom gives 240 cm of his ribbon to Nijah.

How much ribbon does he have left?

How many 10 cm lengths does Tom have left?



Tiny has worked out  $3\text{ m }20\text{ cm} - 2\text{ m }56\text{ cm}$ .

$$3\text{ m }20\text{ cm} - 2\text{ m }56\text{ cm} = 1\text{ m }36\text{ cm}$$

64 cm

What mistake has Tiny made?

What is the correct answer?



# What is perimeter?

## Notes and guidance

In this small step, children are introduced to perimeter for the first time.

Children learn that perimeter is the distance around the outside of a closed 2-D shape. Children explore what perimeter is, and what it is not, by deciding whether they can find the perimeter of a group of open and closed 2-D shapes.

Provide children with practical opportunities to understand perimeter, such as walking around the perimeter of the playground or using their finger to trace the perimeter of 2-D shapes.

At the end of this step, children start to find the perimeter of shapes on squared grids by counting along the edges. Encourage children to mark as they count to ensure they do not miscount.

### Things to look out for

- Children may think that it is possible to find the perimeter of open shapes.
- When children are finding the perimeter of a shape on a squared grid, they may miscount by counting all of the squares around the shape rather than along the edge of the shape.
- Children may trace or count some sides more than once.

## Key questions

- What does “perimeter” mean?
- When might someone need to find the perimeter in real life?
- Why are you unable to find the perimeter of this shape?
- How would you use your finger to trace the perimeter of this piece of paper?
- Which of the shapes has the greater perimeter?  
How do you know?
- How does the squared grid help you to find the perimeter?

## Possible sentence stems

- The perimeter of a shape is ...
- This shape does/does not have a perimeter because ...
- I can find the perimeter of this shape by ...

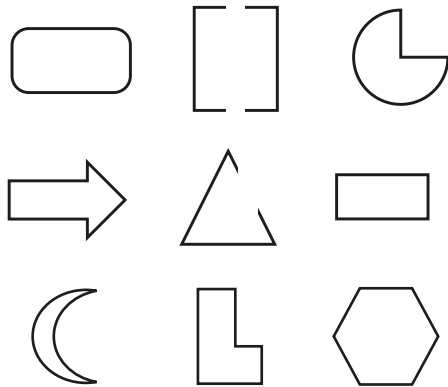
### National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)
- Measure the perimeter of simple 2-D shapes

# What is perimeter?

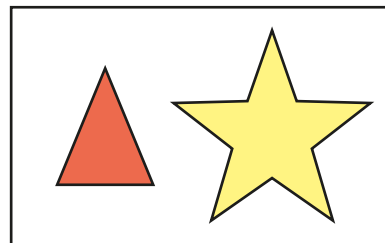
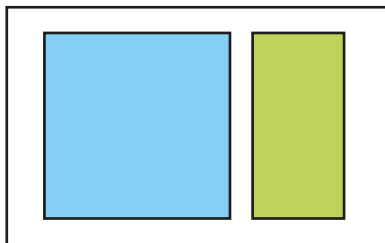
## Key learning

- Which shapes have a perimeter?

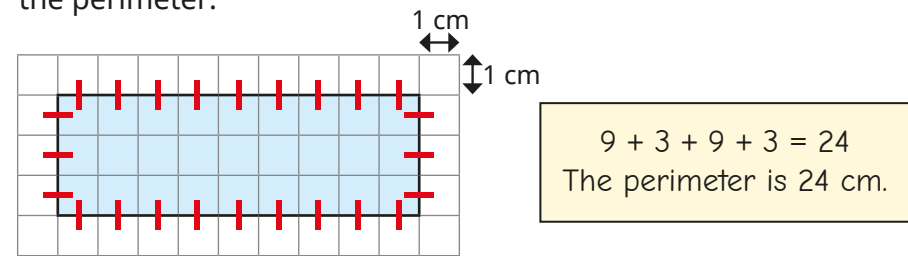


Why do some of the shapes not have a perimeter?  
Compare answers with a partner.

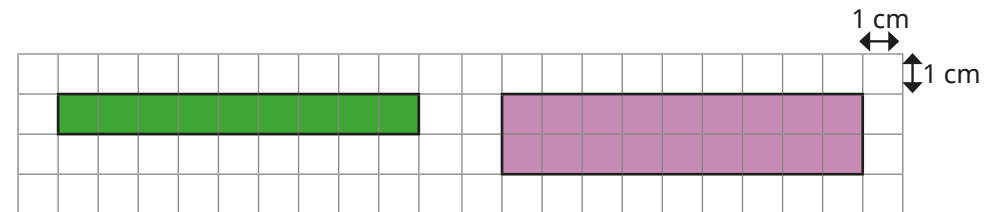
- Which shape has the greater perimeter in each pair?  
How do you know?



- Scott counts around the edge of the rectangle to find the perimeter.

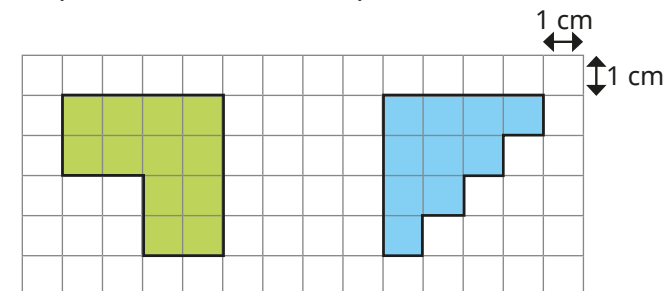


Use Scott's method to find the perimeter of each rectangle.



What do you notice?

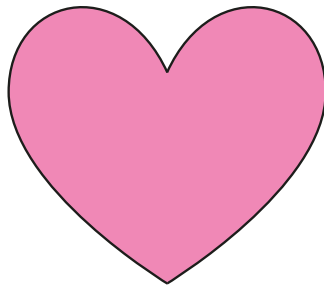
- Work out the perimeters of the shapes.



# What is perimeter?

## Reasoning and problem solving

Whitney wants to find the perimeter of this shape.



I cannot find the perimeter of the shape, because it does not have straight sides.

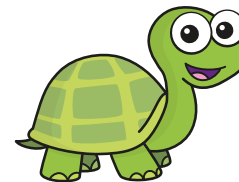
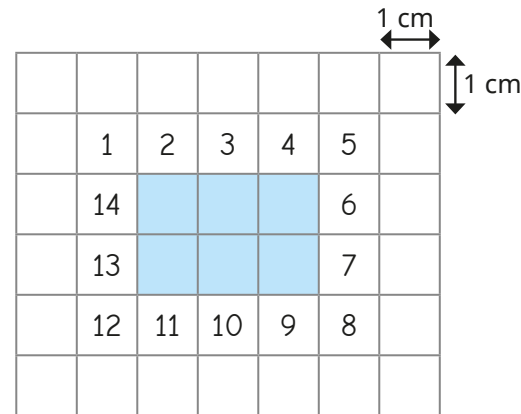


Do you agree with Whitney?  
Explain your thinking.



No

Tiny is finding the perimeter of the shape by counting squares.



The perimeter is 14 cm

What mistake has Tiny made?  
Find the correct perimeter.

Tiny has counted the squares rather than the edges of the shape.

10 cm

# Measure perimeter

## Notes and guidance

In this small step, children measure the sides of different shapes in centimetres to find the perimeter. This builds on the previous step, where children found the perimeter by counting the number of squares of each length.

Encourage children to work in a systematic order, possibly marking the lengths after they have been measured, to ensure that children measure the lengths of all the sides.

Children should also be encouraged to think about whether it is necessary to measure every side to find the perimeter or whether they can use the properties of 2-D shapes to help them.

Children could explore measuring the perimeter of shapes with curved sides by using a piece of wool or string to place along the edges and then measuring the wool or string with a ruler.

## Things to look out for

- When measuring, children may start from the beginning of the ruler, rather than from the zero mark.
- Children may not record the units of measurement in their answer.
- Children may measure using the non-metric side of the ruler.

## Key questions

- What does “perimeter” mean?
- What equipment is useful for measuring the perimeter of a shape?
- Does starting in different places when measuring the perimeter give you a different answer?
- Do you need to measure all the sides? How do you know?
- How do you know that you have measured all the sides?
- Which method do you prefer, to find the perimeter of a square?
- Can you find the perimeter of a shape with a curved edge? How?

## Possible sentence stems

- Perimeter is ...
- \_\_\_\_\_ cm + \_\_\_\_\_ cm + \_\_\_\_\_ cm + \_\_\_\_\_ cm = \_\_\_\_\_ cm

## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)
- Measure the perimeter of simple 2-D shapes

# Measure perimeter

## Key learning

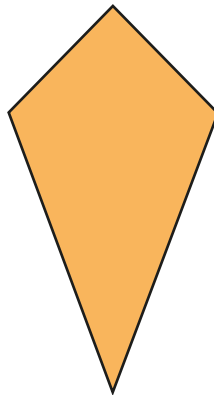
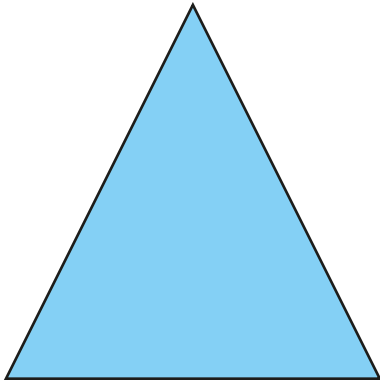
- Measure and label each side of the rectangle.



What is the perimeter of the rectangle?

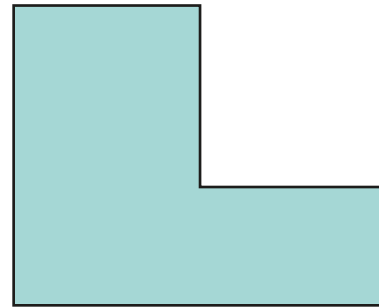
$$\underline{\quad} + \underline{\quad} + \underline{\quad} + \underline{\quad} = \underline{\quad} \text{ cm}$$

- Measure and label the sides on each shape.



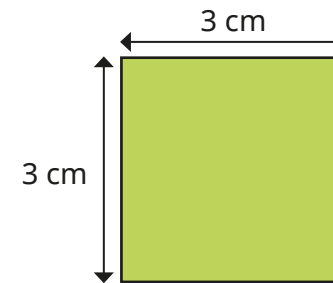
Work out the perimeter of each shape.

- Measure and label the sides of the hexagons.



Work out the perimeter of each hexagon.

- Here is a square.



Do you need to measure all the sides to find the perimeter?

What is the perimeter of the square?

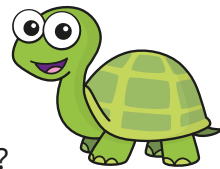
# Measure perimeter

## Reasoning and problem solving

Scott is measuring the perimeter of a rectangle.



Scott only needs to measure two sides!



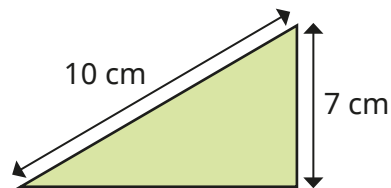
Do you agree with Tiny?

Explain your answer.



Yes

Dexter thinks that the perimeter of the triangle is 17 cm.

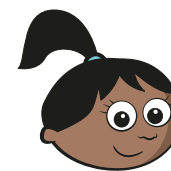
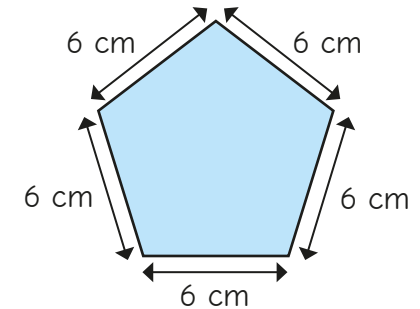
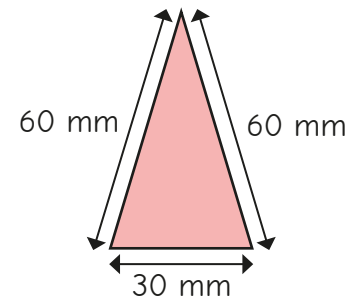


Explain why Dexter is incorrect.

Dexter has only measured two sides of the triangle.

The perimeter is the total distance around the shape.

Sam measures the sides to find the perimeters of the shapes.



The perimeter of the triangle is greater than the perimeter of the pentagon.

What mistake has Sam made?

The units of measurement are different.  
triangle = 15 cm; pentagon = 30 cm



# Calculate perimeter

## Notes and guidance

In this small step, children use their understanding of the properties of different shapes to calculate the perimeter of simple 2-D shapes.

Encourage children to identify equal sides of a square and equal opposite sides of a rectangle to support them in calculating the perimeter. It is important to explore different strategies for calculating perimeter with children and encourage them to use more efficient strategies, for example for a rectangle they could add all four lengths, they could double the width and length and add them together or they could add the width and length and then double.

Although children can calculate the perimeter of rectilinear shapes in this step, these shapes are not formally introduced until Year 4

## Things to look out for

- Children may not record the units of measurement in their answer.
- Children may not remember that a square has four equal sides and that opposite sides of a rectangle are equal.
- Children may find it difficult to add lengths measured in centimetres and millimetres.

## Key questions

- Are any of the sides equal?
- How can you work out the perimeter of the shape?
- What other method could you use to find the perimeter of the shape?
- How can you work out the lengths of the sides that are not labelled?
- How many sides do you need to measure before you can find the perimeter?
- Do the lengths need to have the same unit of measurement? How do you find equivalent lengths?

## Possible sentence stems

- Opposite sides of a rectangle are \_\_\_\_\_
- The missing side length is \_\_\_\_\_ cm because ...

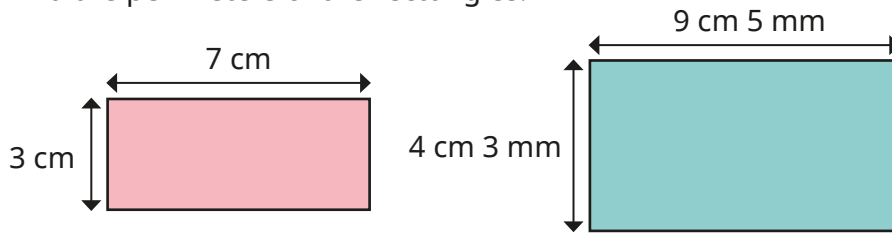
## National Curriculum links

- Measure, compare, add and subtract: lengths (m/cm/mm); mass (kg/g); volume/capacity (l/ml)
- Measure the perimeter of simple 2-D shapes

# Calculate perimeter

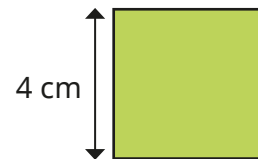
## Key learning

- Find the perimeters of the rectangles.

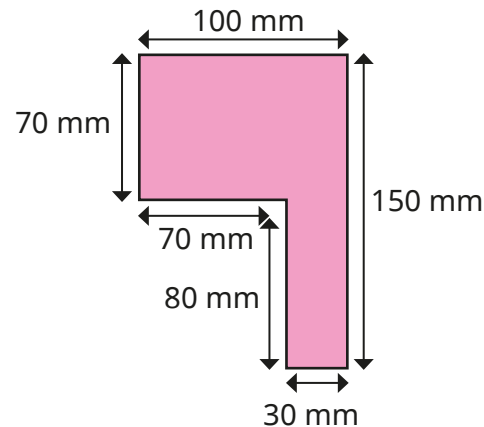
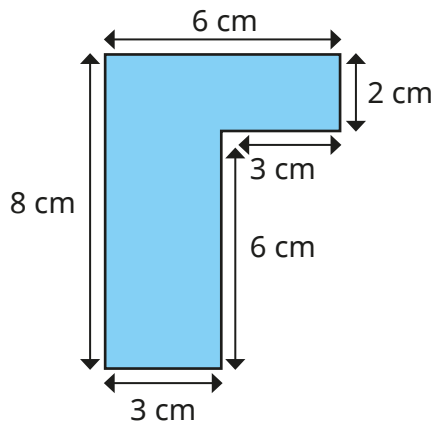


Compare methods with a partner.

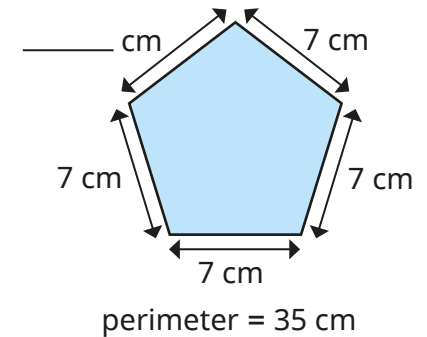
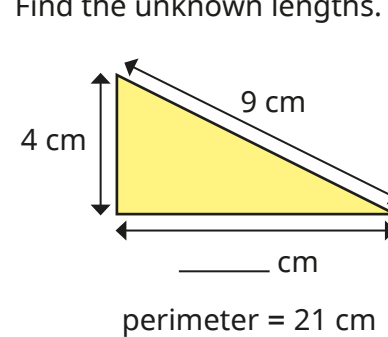
- Find the perimeter of the square.



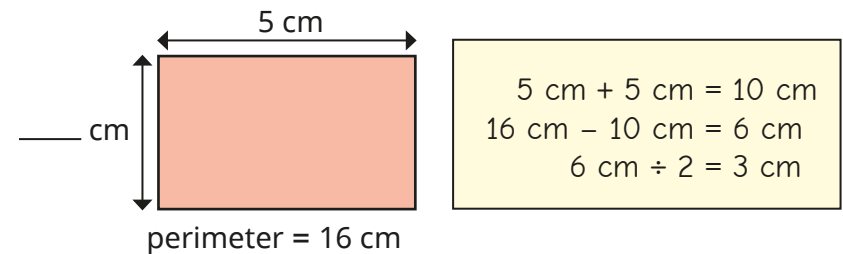
- Work out the perimeter of each shape.



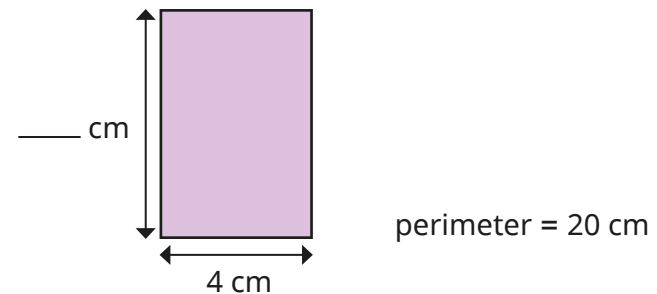
- Find the unknown lengths.



- Esther is finding the unknown length of the rectangle.



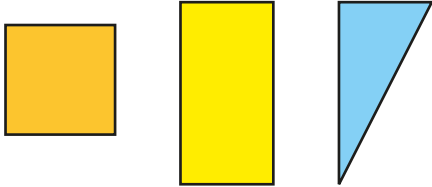
Use Esther's method to find the unknown length.



# Calculate perimeter

## Reasoning and problem solving

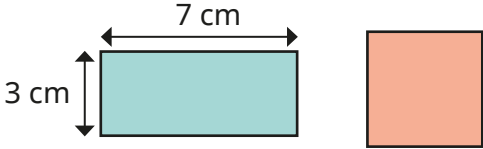
How many sides do you need to measure to find the perimeter of each shape?



Explain your answers.

square: one side  
 rectangle: two adjacent sides  
 triangle: all three sides


The rectangle and square have the same perimeter.



What is the length of each side of the square?

5 cm

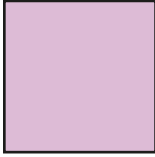
Each side of this shape is the same length.



The perimeter is 60 cm.  
 How long is each side?

6 cm

The perimeter of the square is greater than 11 cm and less than 25 cm.



In whole centimetres, what could the length of one side be?

3 cm, 4 cm, 5 cm or 6 cm